



February 7th, 2020 | 12:00 PM – 01:00 PM (EDT)

Mathematical modelling of skin absorption and transport

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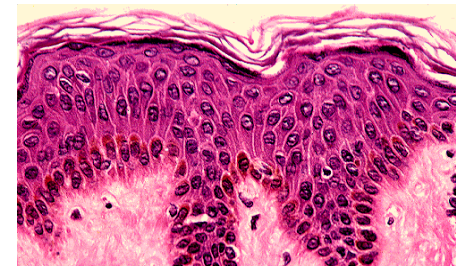


Learning objectives

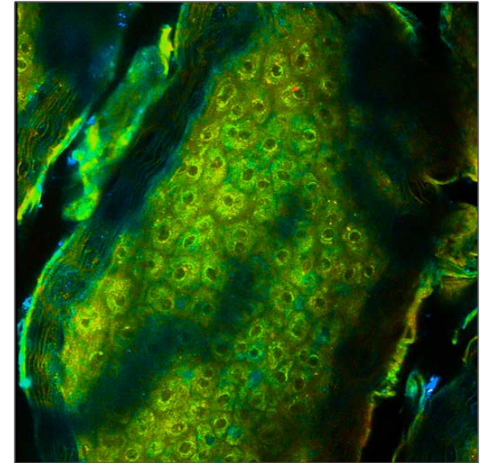
Outline

- Why do we need mathematical modelling in skin absorption & transport?
- Understand limitations of top down, bottom up & middle out approaches to studying skin drug absorption & subsequent effects
- Apply mathematical modelling principles to transdermal & topical absorption

H& E histology of skin



Multiphoton image of skin



Applying product to skin



Why do we need mathematical modelling in skin absorption & transport?

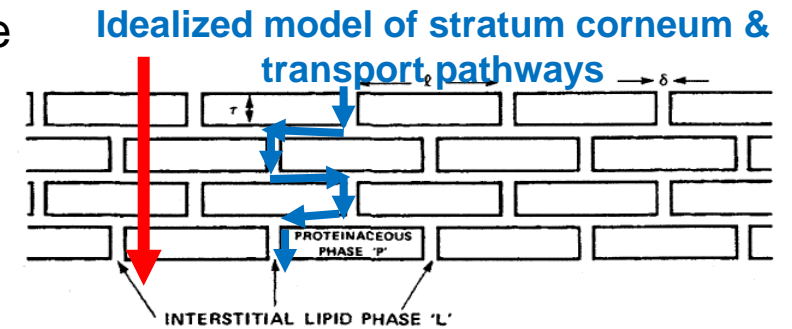
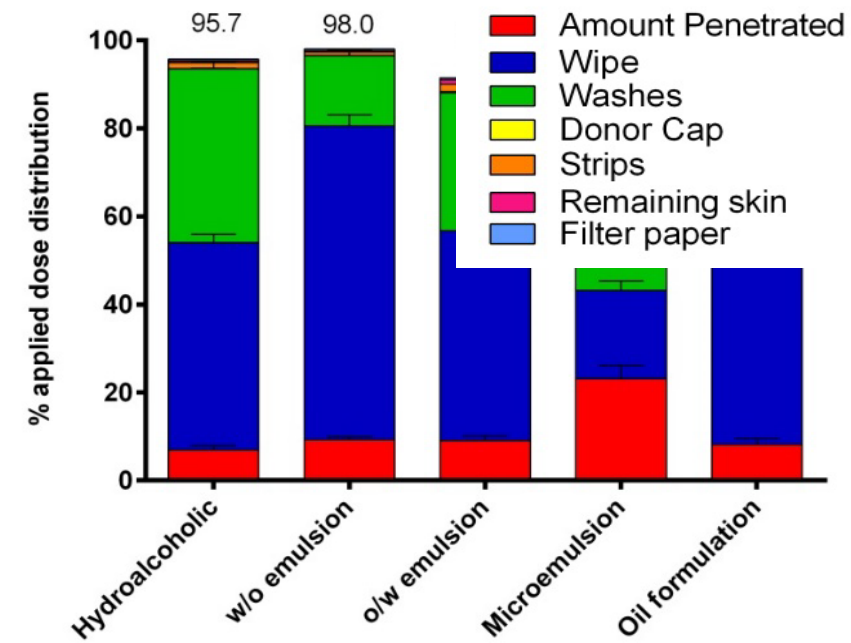
- As one example, a graphical representation of concentration versus time or, as shown on right, of mass balance of *IVPT* finite dose testosterone data is the simplest way of summarising & visualising actual data
- A mathematical model may be a simple or complex representation of what may be occurring and may have the additional benefit of being able to predict and be extrapolated beyond the data available to other situations,
- However,
- All models are wrong, but some are useful*

Box, G. E. P. *J Amer Stat Assoc*, 71 (356): 791–799, (1976)

BUT

Everything should be made as simple as possible, but not one bit simpler.

Attributed to Albert Einstein, 1879 – 1955



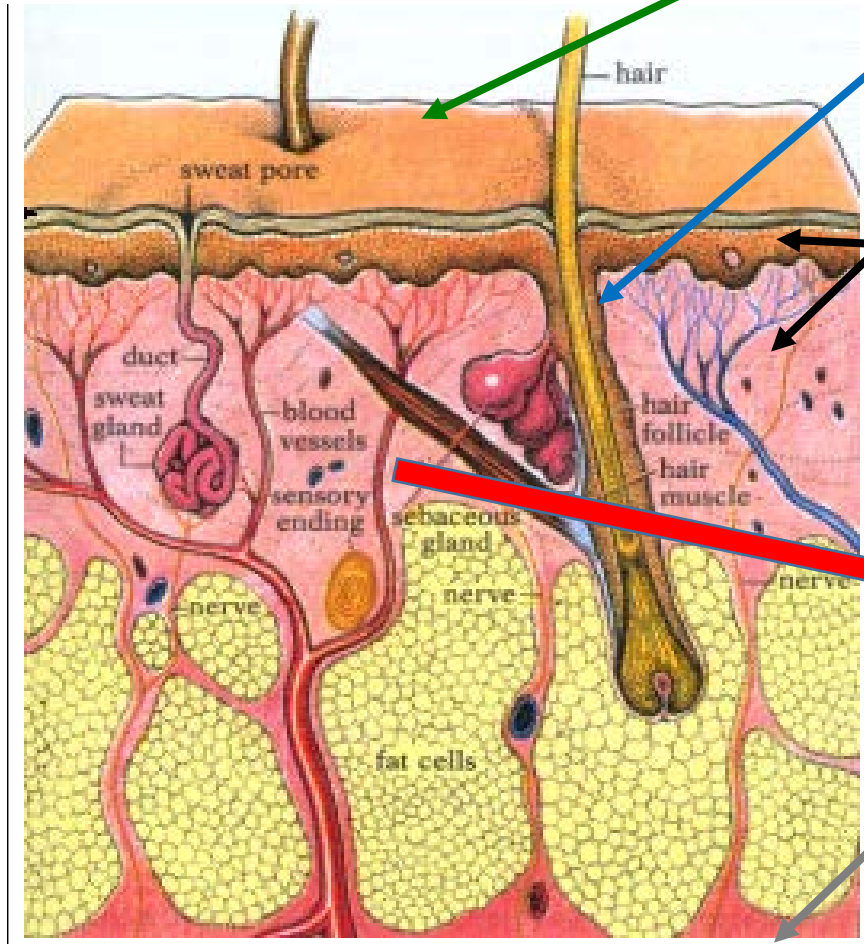
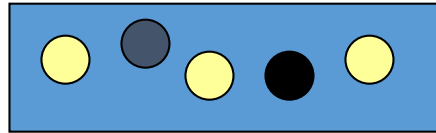
Intercellular localisation of n-butanol in intercellular SC lipids



Nemanic & Elias. *J Histochem Cytochem* (1980) **28**: 573-8

Our focus here is using models to assess delivery to our target sites with topical or transdermal products

Product

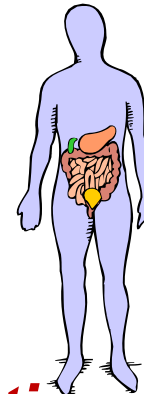


Superficial – *retention & action*

Appendageal – *targeting, adequate concentration, retention*

Epidermal/ Dermal
– *effective concentration to modulate keratinocytes, immune/inflammatory & other cells;*

Systemic



Nitroglycerin, scopolamine
nicotine, HRT, long duration,
avoid git first pass, manage
nausea etc

Deep Tissue – *effective concentration to modulate muscle inflammation*

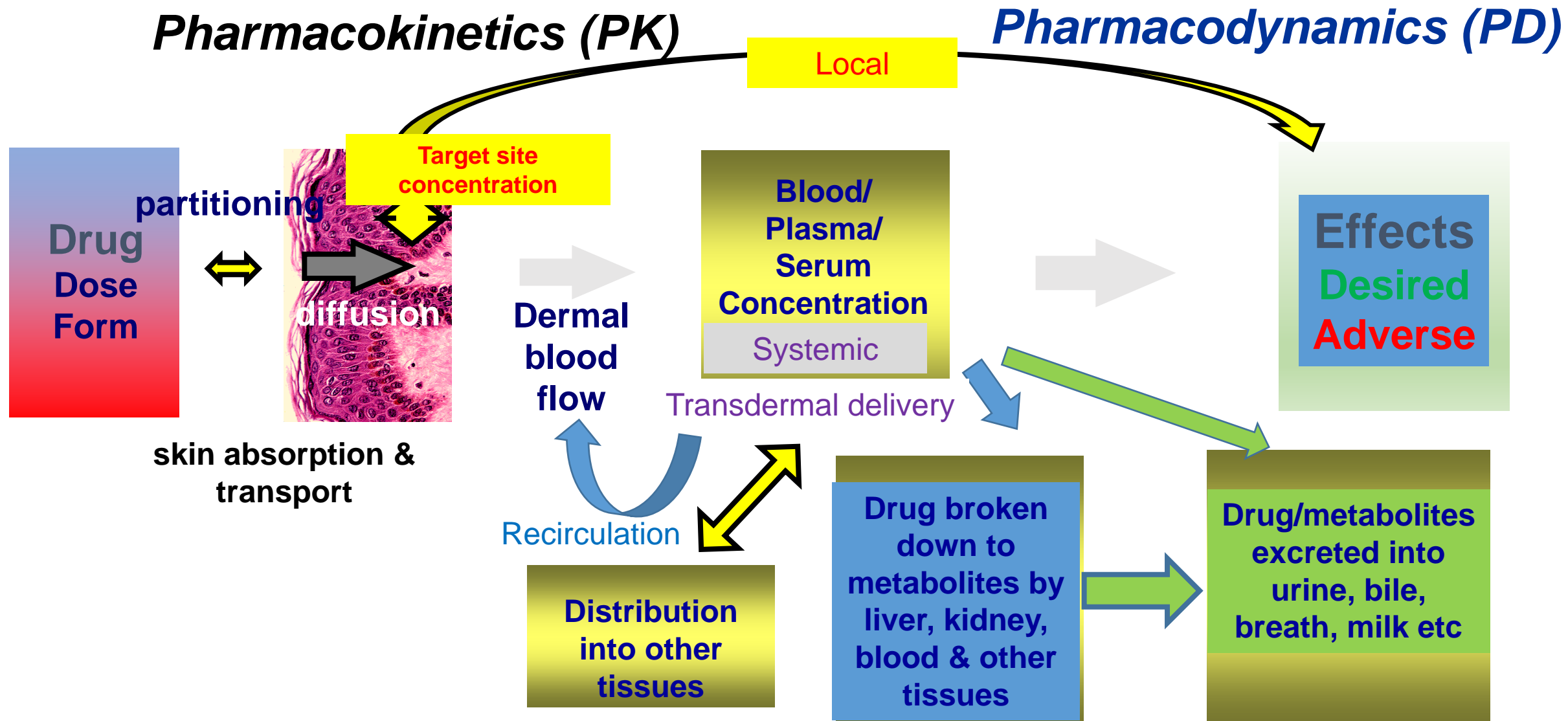
Barrier products,
sunscreens,
insect repellents,
cosmetics

Anti-acne,
anti-perspirants,
hair restorers

Steroids, anti-
histamines, local
Anaesthetics, ant-
infectives

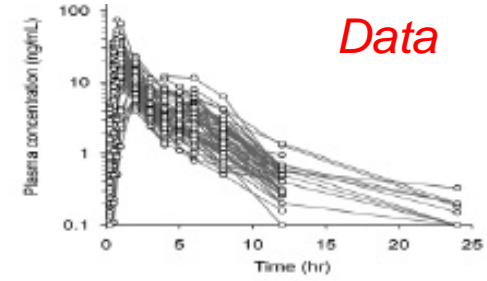
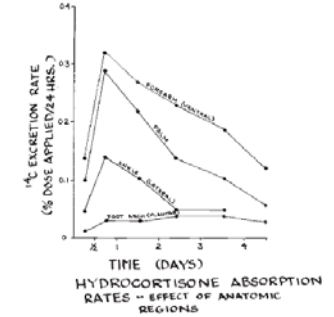
Analgesics
anti-inflammatories

Framework for mathematical modelling in skin absorption & transport



An over-riding consideration in assessing whether we can achieve targeted delivery is appropriate modelling

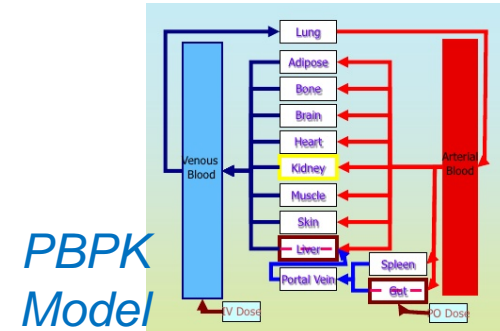
- Currently three data driven approaches:
 - The “top-down” approach, in which **pharmacometrics** (often dominated by statistics) is used to model, interpret both *in vivo* and *in vitro* data, and relate *in vivo*, *in vitro* and *in silico* data in both understanding & predicting *in vivo* skin absorption and transport for various products,
 - The “bottom-up” approach whereby a **mechanistic understanding of the interactions and temporal changes in active-product-skin interactions** and the processes of topical absorption can be used to explain and predict skin absorption and transport, and
 - **A bringing of the two streams together – the middle out approach.**
- In doing applying these models, we need to keep in mind an old saying that really underpins our work:
 - *It is better to be approximately right than absolutely wrong – Brian Barry*



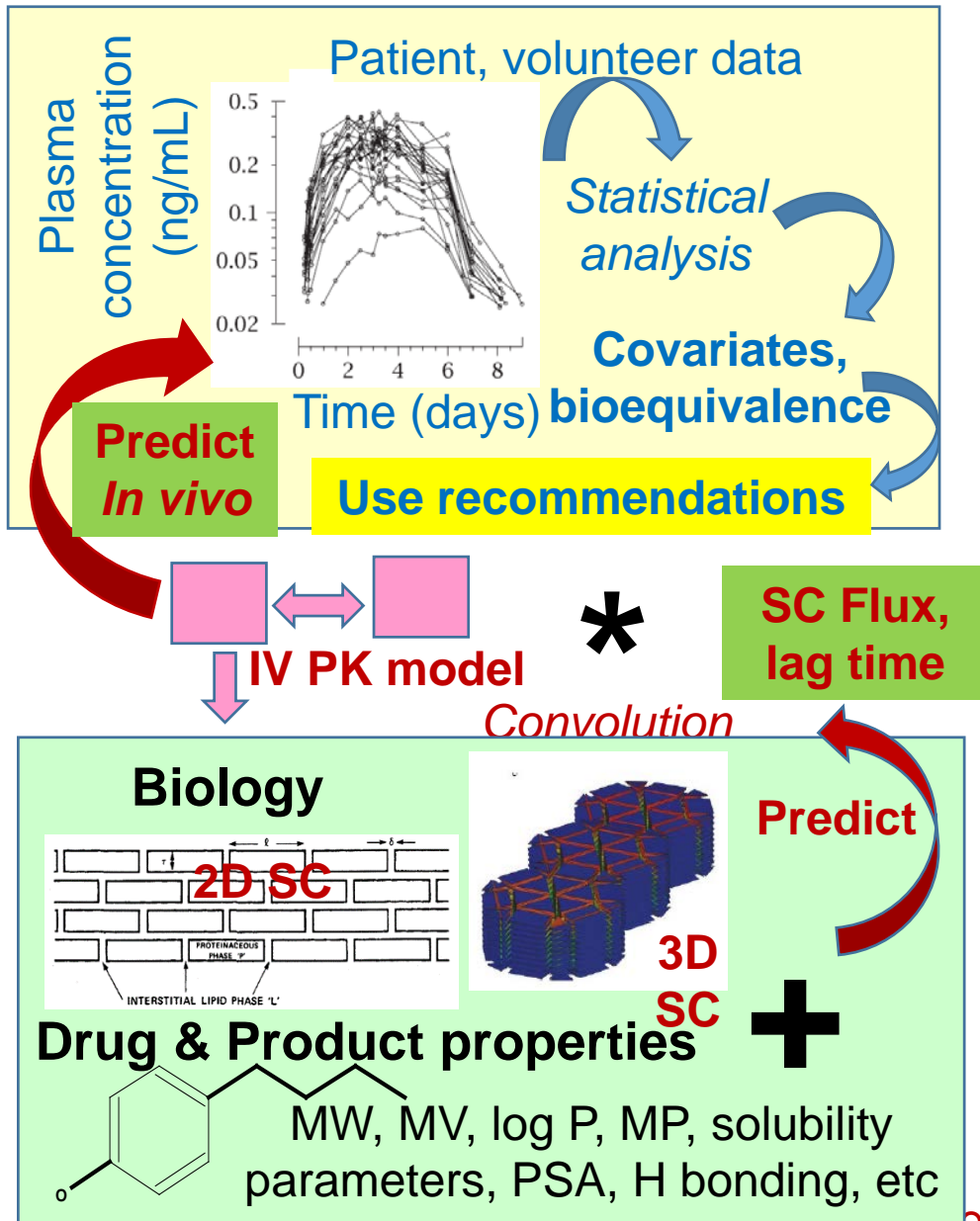
Assume no model or use simple PK compartment

Analyse

Predict
Convolute with skin PK model



Top-down & bottom up approaches



Top - down

- Collect *In vivo* human exposure & response data
- Use ‘mixed model’ or other analyses to identify key co-variates in topical drug exposure & response
- Analysis by non-parametric, by a plausible pharmacokinetic &, if population data, population pharmacokinetic - pharmacodynamics model

Focus on confirming and defining clinical usage conditions

Focus on predicting, learning and translation

- ❖ Link predictions to systemic blood/local levels & effects
- ❖ Physiologically based pharmacokinetic (PBPK) model for skin, target & disposition to predict *in vivo*
- ❖ PBPK model (s) for skin to predict *in vitro* absorption
- ❖ *In vitro* physiochemical data of solutes, product formulation & skin morphology

Bottom - up

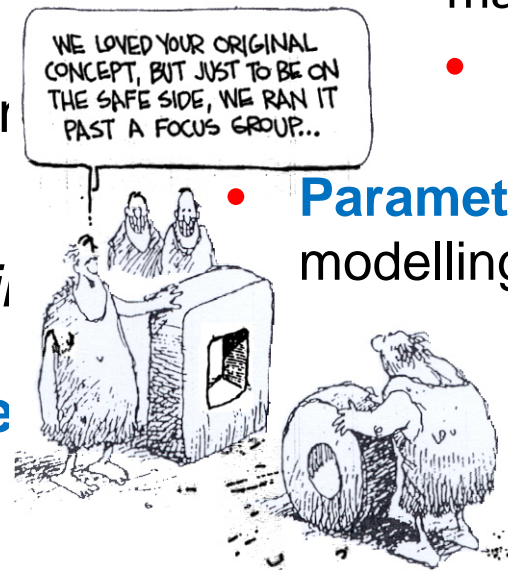
My thoughts on advantages & dangers in modelling skin absorption

Advantages

- ✓ Growth of computer science & *in silico* modelling means **low cost & fast** outcomes
- ✓ Able to use known, rich morphology & pharmacology to **predict effects in inaccessible topical action sites**
- ✓ Avoid *in vivo* studies
- ✓ Prediction accuracy by *in vitro-in vivo* extrapolation (IVIVE) methods
- ✓ Virtual models yield robust statistical analysis eg bootstrapping
- ✓ **Predictive performance** of formulation design & release profiles
- ✓ **Translation of data** to predict local PKPD at a target site using IVPT and *in vivo* sampling from another body site
- ✓ Modelling to take into account **disease effects** & abnormal kinetics

Dangers

- **Model** is **plausible** in biology & thermodynamics
- Poor **structural identifiability** (eg can an unknown parameter be identified by experiment is assumption that corneocyte wall offers no barrier resistance real!!)
- **Lack of sensitivity** due to limited data or in PBPK model predictions – PBPK sensitivity analyses with varying parameters critical
- **Correlation between PBPK parameters**, eg half life = $0.693 V_d/\text{clearance}$; permeability coefficient $k_p = \text{maximum flux/saturated concentration}$
- **Variability** – in skin type, disease, study design, environment, genetics
- **Parameter uncertainty** (experimental, modelling & assumption errors) – Bayesian best!
- **Extrapolating beyond** data,
- **Group think** – permeability coefficients, normal SC, lipid pathway, transcellular pathway etc

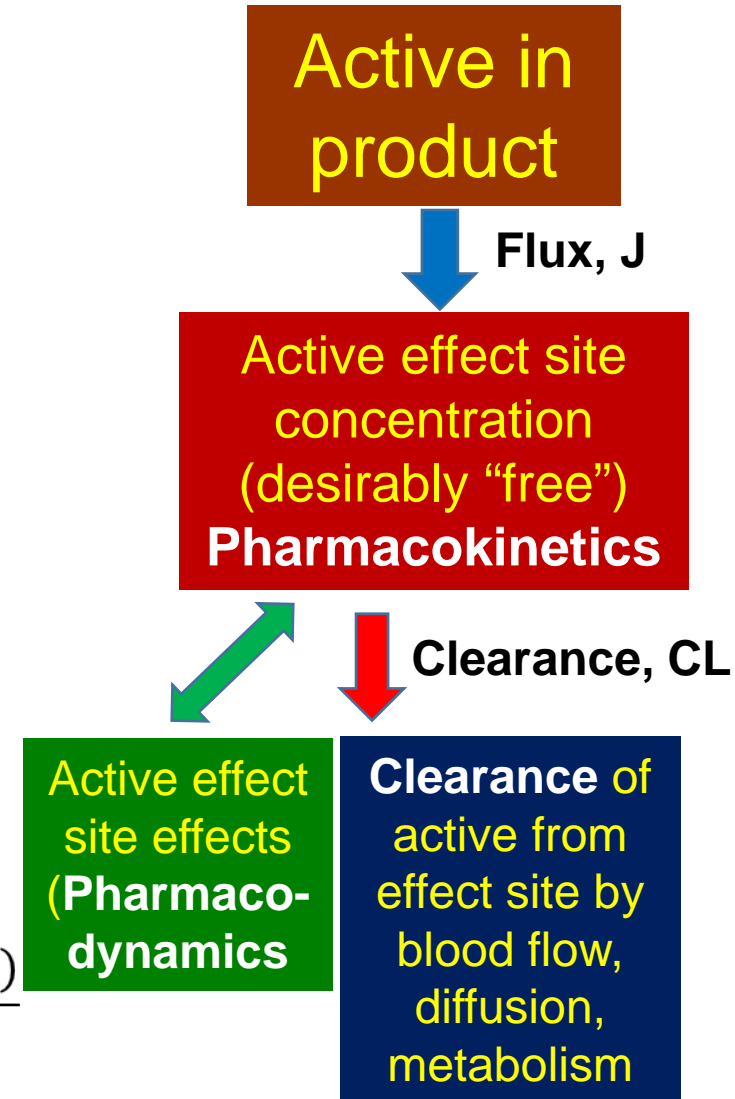


General pharmacokinetic principles often apply in topical delivery, but with incomplete release

- Two key goals in topical drug delivery are to:
 - Quantify the **extent and rate of absorption** of an active drug to a topical target site (bioavailability) and
 - Express topical delivery in terms of its **target site effect** (may be local or use blood level as a surrogate) and unwanted absorption and potential toxicity (may be systemic).
- Quantification of **extent and rate**
 - **Extent** is best expressed as an **amount absorbed over a time period**
 - ❖ % absorption, although commonly used, can be misleading as amount absorbed often not proportional to dose applied
 - ❖ Area under the curve for a blood concentration –time or response –time (eg vasoconstrictor test) often used as surrogates
 - **Rate** can be defined as continuous or as a peak rate/ concentration & peak time
 - ❖ Continuous rate defined as steady state flux (J_{ss})
 - ❖ Maximum flux (J_{max}) is that obtained under thermodynamically stable conditions for the equivalent of a saturated solution.

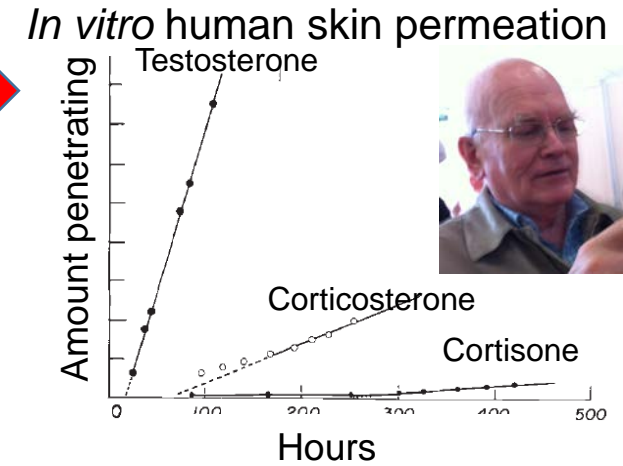
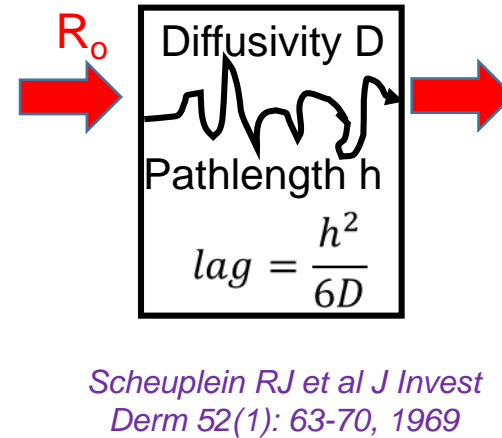
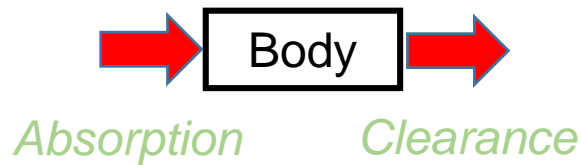
Effect is usually expressed in terms of “unbound” or “free” effect and toxic site concentrations

$$\text{Steady state concentration at a given site } C_{ss} = \frac{\text{Rate of delivery to that site (flux)}}{\text{Clearance from that site (CL)}}$$

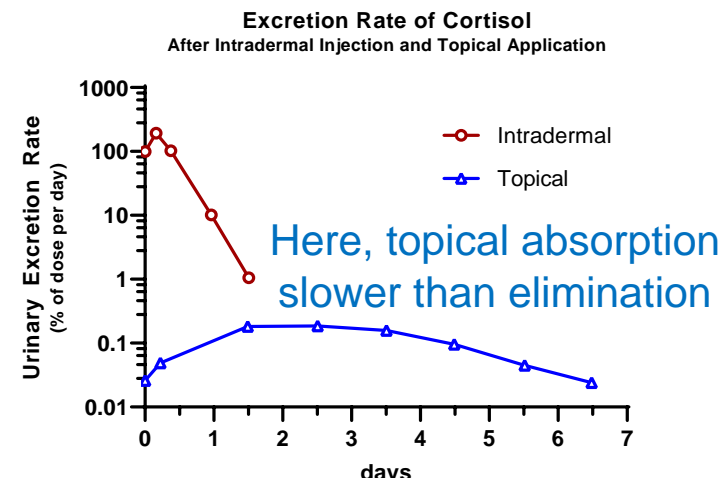
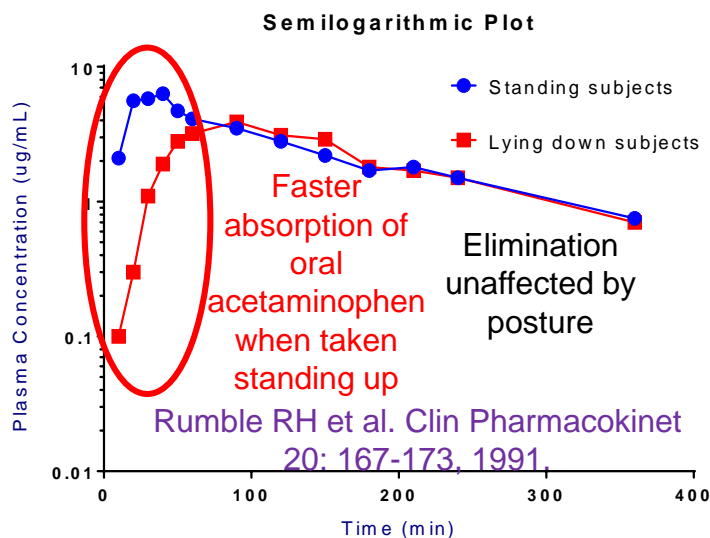


Additional general mathematical modelling (PKPD) principles applying to topical & transdermal product delivery

- There is a **lag time** for drugs diffusing across the quite effective SC barrier
- Usually the absorption rate of a drug is faster than its elimination



- In contrast, absorption across the skin is usually slower than its elimination from the body – the so-called **flip-flop effect!**

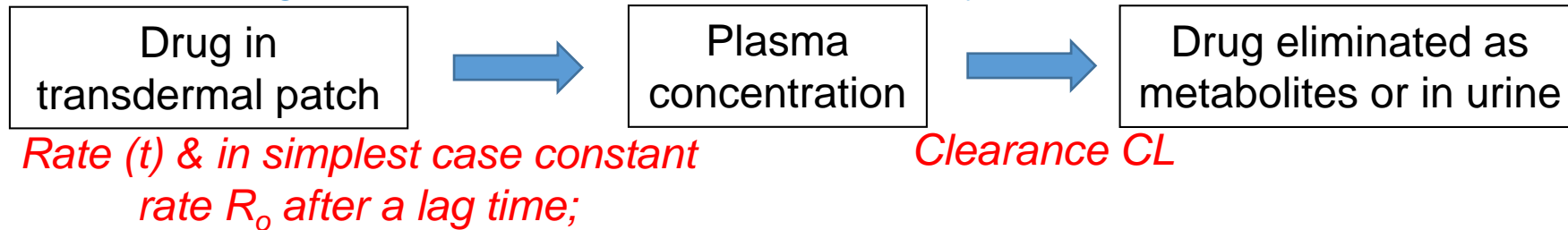


Riegelman S. Clin Pharm Ther 16: 873- 883, 1974



Transdermal delivery

Steady state plasma drug concentrations can be described by a simple input – elimination model



In multiple dosing, $R_o = \frac{\text{Dose delivered per patch}}{\text{Dose interval between patches, } \tau}$

Transdermal products popular as:

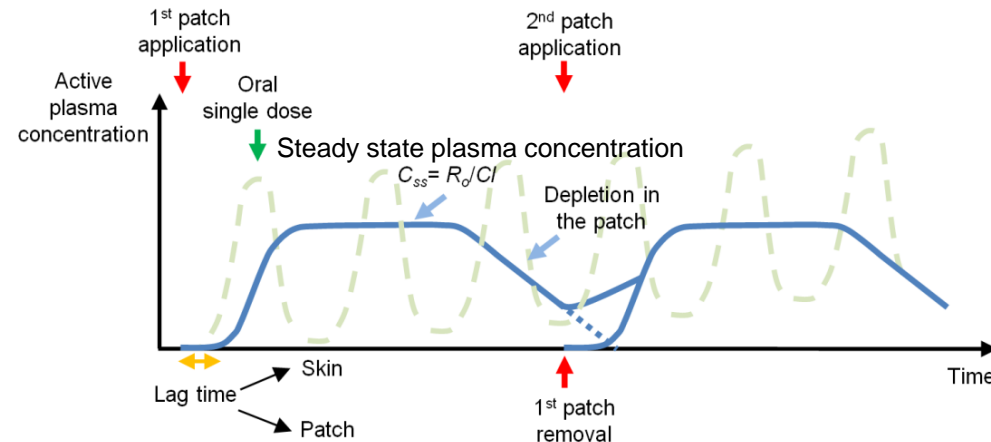
- Avoid first pass, plasma level fluctuations & gastric distress associated with some oral products
- Are easily removed should there be any toxicity
- In some cases, cause systemic toxicity

As the target steady state plasma concentration C_{ss} to be effective and safe is defined by: $C_{ss} = \frac{R_o}{CL}$

The desired transdermal delivery rate, $R_o = CL \cdot C_{ss}$

Actives must be

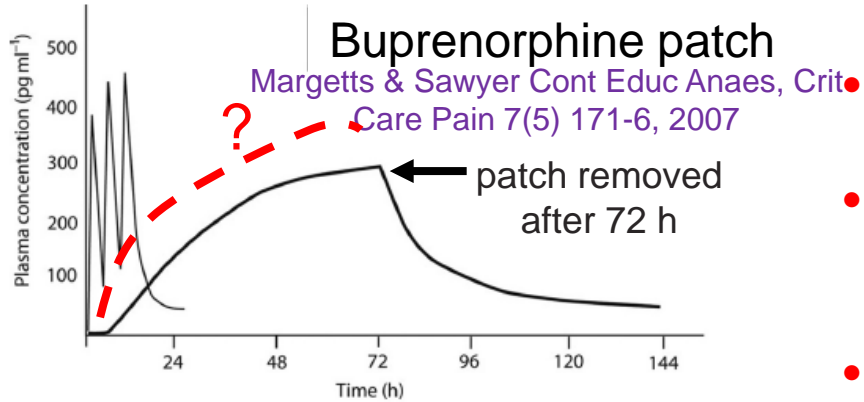
- Potent
- Have an adequate skin absorption rate (the upper rate defining skin reactions)
- Not be cleared too rapidly



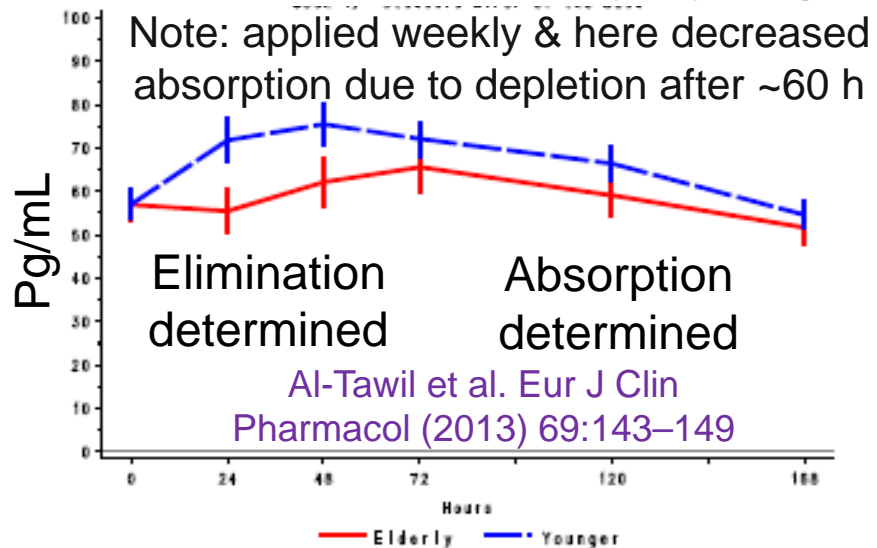
Pastore et al BJP 172(9):2179-209, 2015

Note: more complex model needed to describe full profile

Buprenorphine patch PKPD mathematical modelling



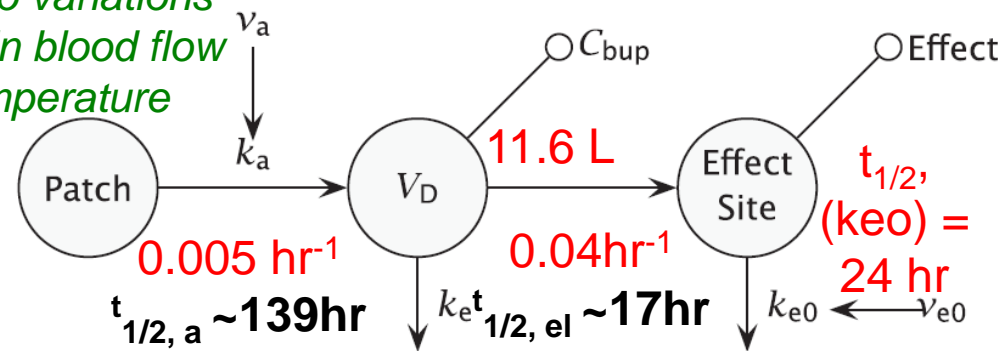
Transdermal buprenorphine patch plasma levels (mean ± se) in elderly & young



Flip-flop kinetics

- At first glance, the sublingual looks like fast absorption & fast elimination
- So that the patch profile reflects a short lag and then patch depletion over time.
- But, look more closely – is there accumulation arising from a long elimination half life?
- Buprenorphine has a half life ($t_{0.5}$) of 24 - 48hr in various patients.
- Its patch should take 3.3 half lives (i.e. 80 – 158 h) to get to 90% C_{ss} with constant R_0

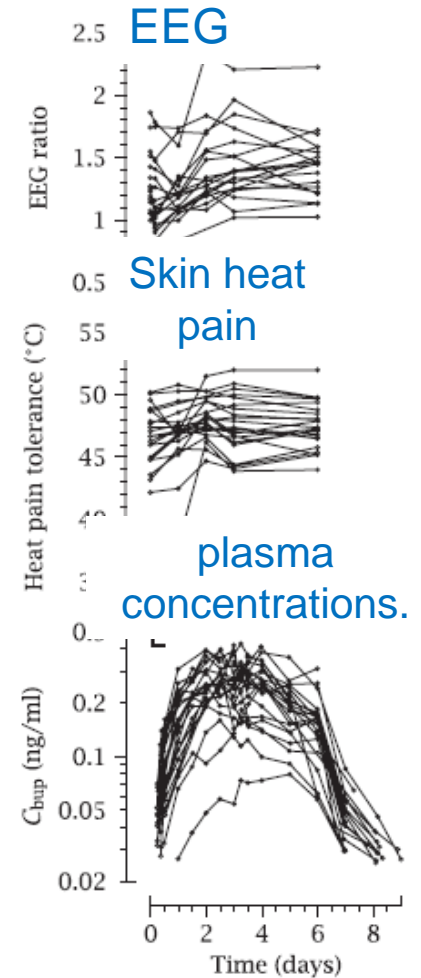
Process noise due to variations in skin blood flow & temperature



Population pk analyses with NONMEM's subroutine ADVAN13, with PK and PD data analyzed simultaneously

PKPD modelling of 144-h (6-day application) data

Individual data

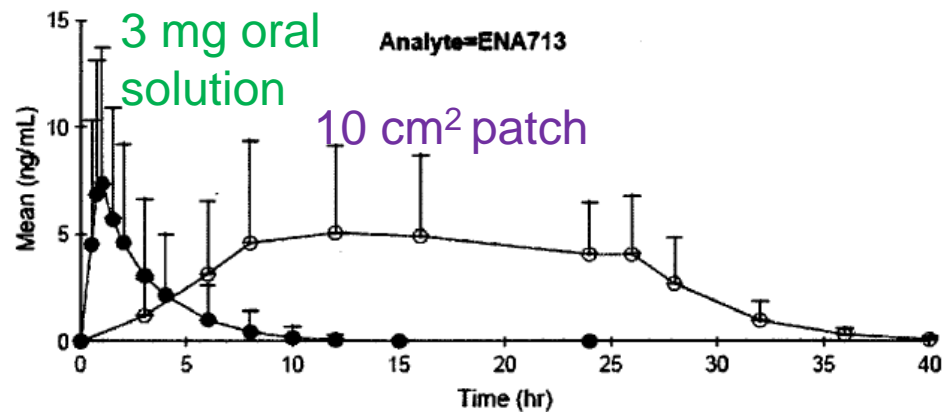


As another example, let us consider the PKPD of rivastigmine approved by the FDA

Centre for Drug Evaluation & Research -Clinical Pharmacology & Biopharmaceutics
Review # 22-083 Exelon^R transdermal patch (Novartis)

- Extension of oral products; doses of 5 cm² (9mg) and 10 cm² (18mg) with a 50% bioavailability for symptomatic treatment of Alzheimer's & Parkinson's disease dementia
- Once a day without food to improve caregiver & patient convenience & as an alternative with swallowing difficulties

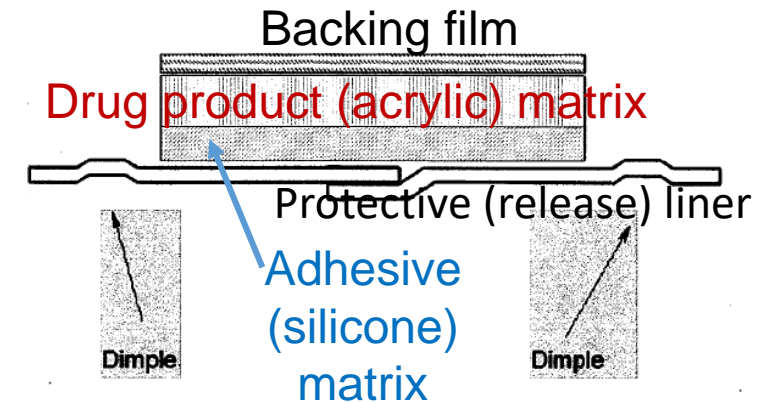
Figure: Rivastigmine plasma concentrations (mean +/- SD) following single dermal (o.d.) patch application (open circles)



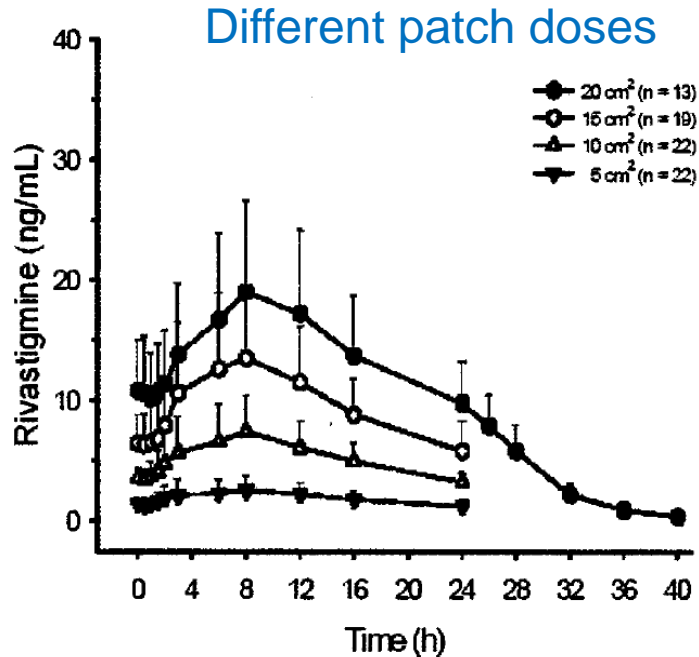
○—10 cm² (FMI) transdermal patch ●—single 3 mg Exelon oral solution

Studies in 440 volunteers & 1374 Alzheimer's patients

Measure AUC₀₋₂₄; C_{max}; t_{max}; t_{1/2}; V/F; CL/F for different doses & with BW adjustment



Exelon^R transdermal patch (Novartis) contd 2



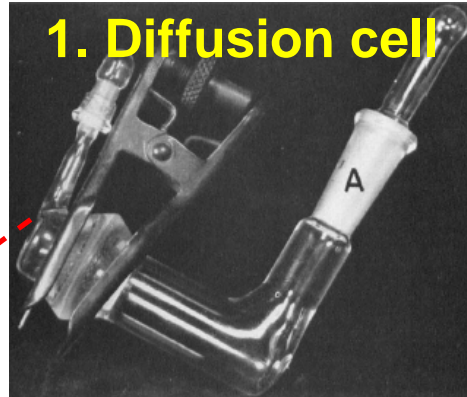
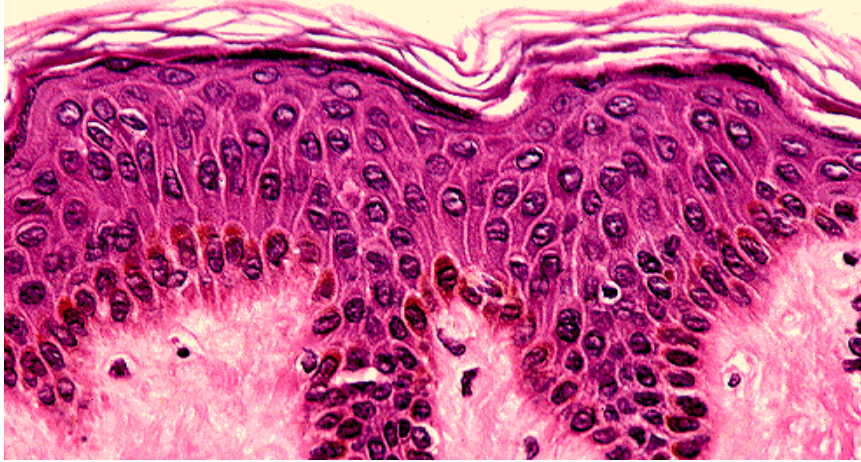
Conclusion: No dose adjustment needed except when titrating low body weight patients with patch doses >10cm²

Population PK analyses of steady state plasma rivastigmine concentrations after patch application

- Renal - no clear effect of creatinine clearance
- Hepatic - no clear effect of SGOT and SGPT
- Age – Study 2320 showed not affected by age (p=0.72)
- Gender – 107 males and 203 females not affected (p=0.73)
- **Body weight – yes p=0.0003**
- Race? P=0.05 but if exclude 2 black patients, p=0.38
- Drug interactions – mainly metabolised by esterase hydrolysis; limited affinity for major CYP450 enzymes

Stratum corneum, SC, is main skin barrier

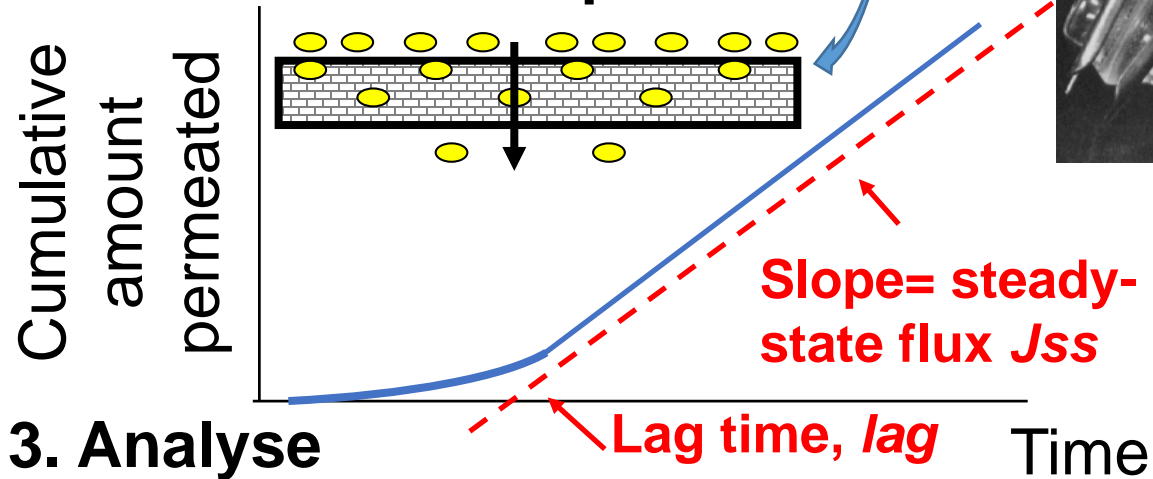
Prediction of human skin permeability of topical & transdermal products using *in vitro* permeation tests (IVPT)



Focus on deriving permeability constant, k_p , *Scheuplein Skin Pharmacol Physiol* 2013;26:199-212



2. Collect data and plot



$$J_{ss} = \frac{Q_{ss}}{A(t-lag)} = \frac{D}{h} (C_{sc,v} - C_{sc,d}) \approx \frac{KD}{h} \Delta C_v = k_p \Delta C_v \approx k_p C_v$$

3. Analyse

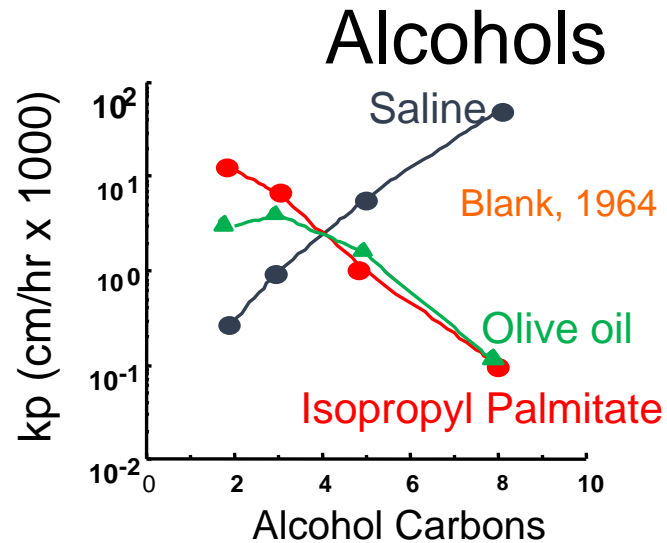
Note steady state diffusion realises:

1. From a **structural identifiability viewpoint** only **2 unique parameters** k_p & lag , which, in turn:
2. Are **highly correlated** - both depend on D , and,
2. Both also have high a **uncertainty**, especially **lag!**

- ✓ Stratum corneum rate limiting
- ✓ Steady state conditions
- ✓ Infinite sink
- ✓ Normally, an aqueous vehicle

Personally, I think that k_p is the wrong paradigm to be using in describing the delivery of actives from products?

k_p paradigm



Impact of formulations on k_p

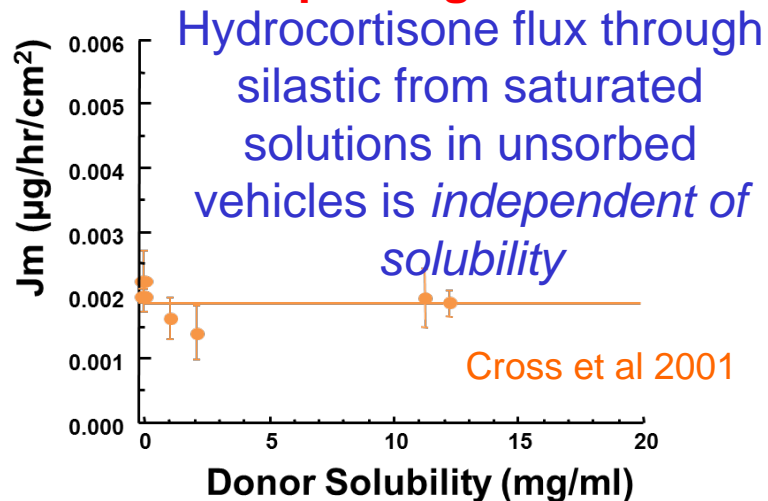
- It is evident here that the more lipophilic solutes have a higher k_p in water where they are less soluble than more polar solutes but the converse applies in oils.



So, what is the alternative paradigm?

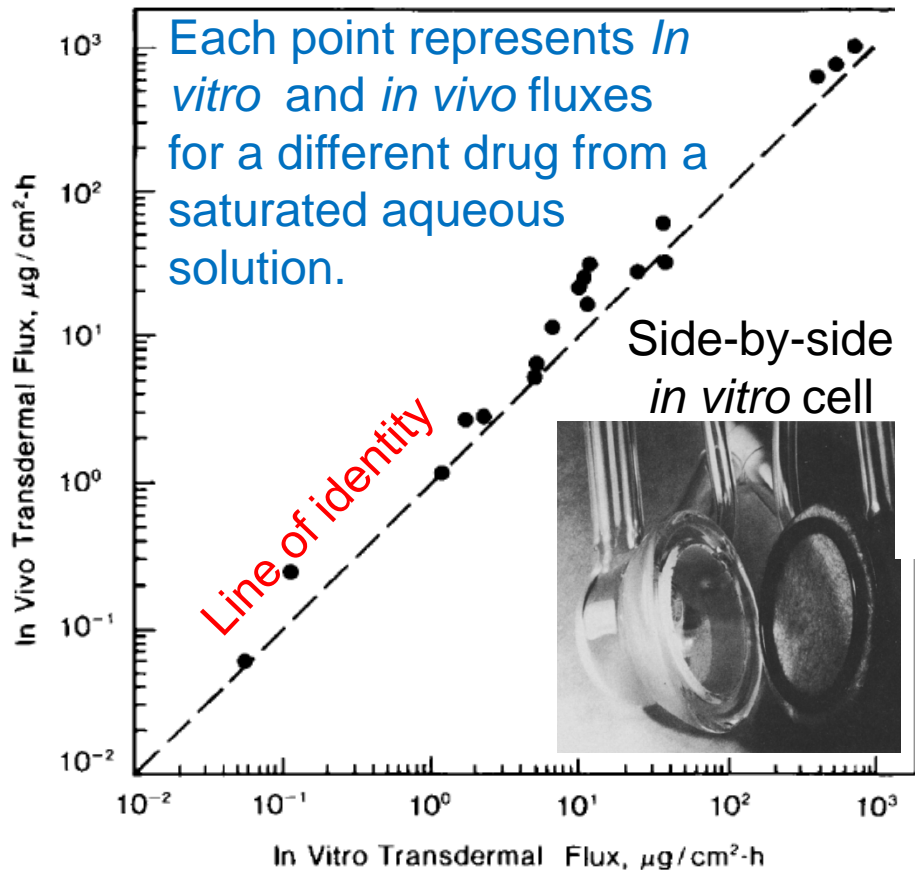
- Back in 1960 in the J Soc Cosmet Chem, Tak Higuchi noted that the thermodynamic activity of a saturated solute in different solvents or in solid form is identical & maximal, unless supersaturated.
- Accordingly, an active should have the same flux for a given fractional solubility in all vehicles, providing that vehicle does not affect the skin & behaves ideally.
- Note: $k_p = \text{Saturated flux} / \text{solubility}$

Max flux paradigm



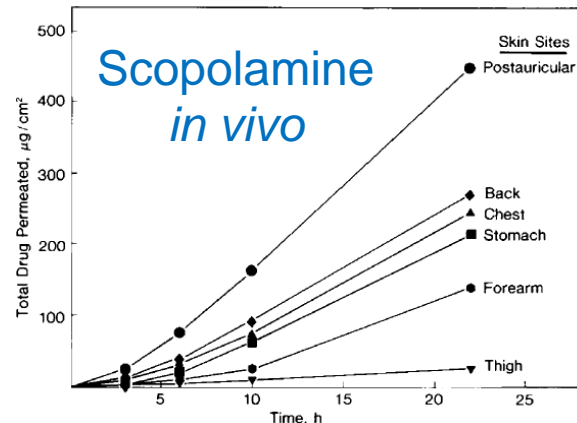
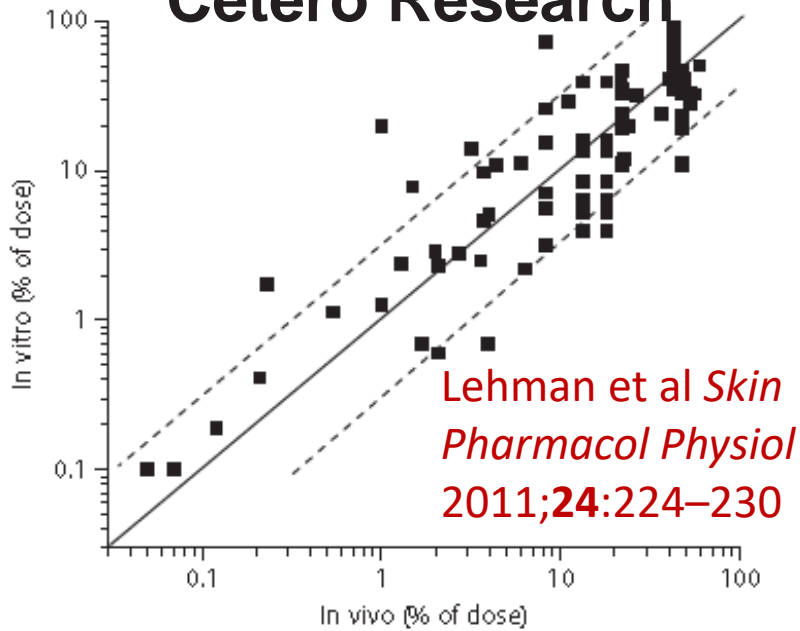
Principles well established that we can use *IVPT* data to predict *in vivo* relationships - but with issues!

Early work by ALZA



Shaw et al *Arch Dermatol* 1987;123:1548-1556

Cetero Research

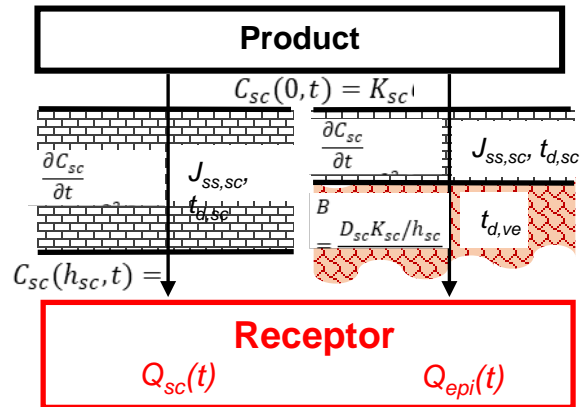


- Lehman *IVIV* 20X difference reduced to <2X with harmonised sets, notably in body sites & product content
- Point-to-point (Level A) with internal & external validation preferred – using *in silico* for skin temperature, metabolism & blood flow, desquamation effects

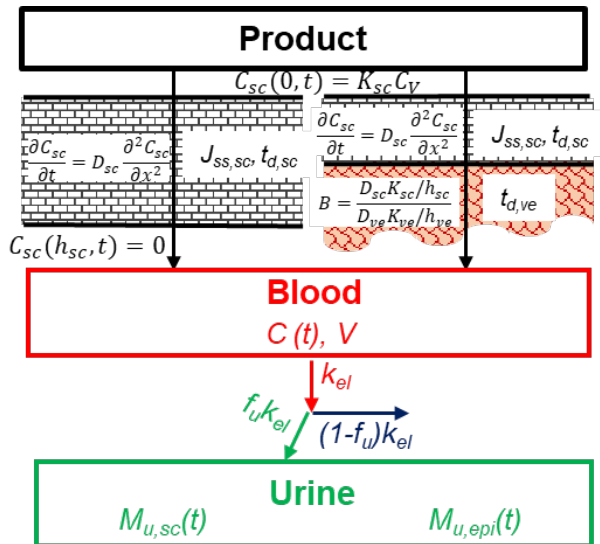
www.fda.gov/downloads/drugs/guidances/ucm070239.pdf

Some examples of PBPK modelling to successfully predict *in vivo* pharmacokinetic profiles from *in vitro* permeation tests (IVPT)

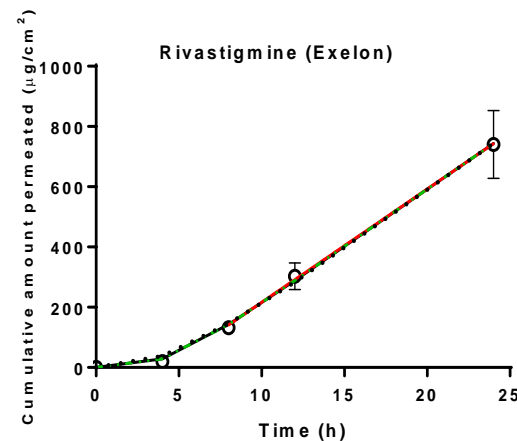
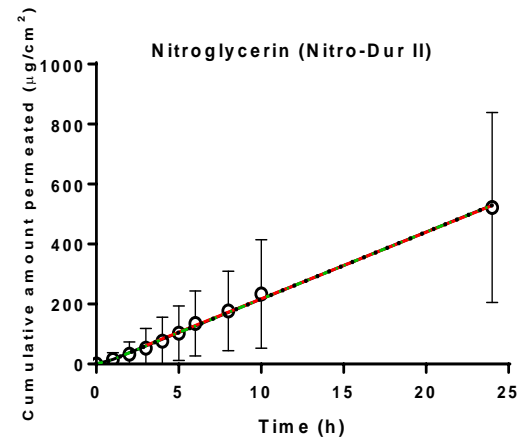
A. SC and epidermal IVPT diffusion model



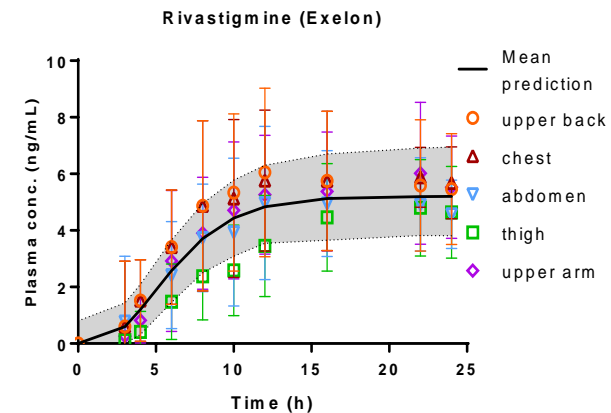
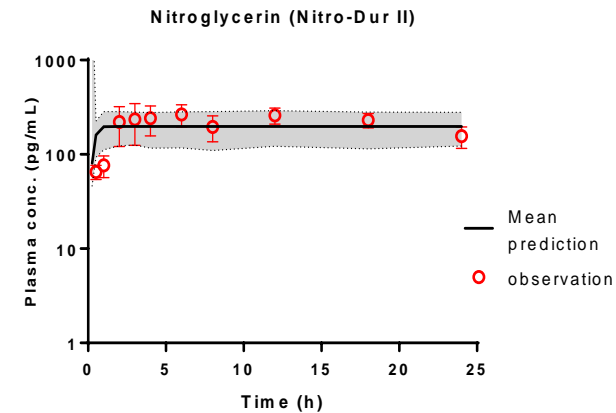
B. SC and epidermal *in vivo* diffusion model



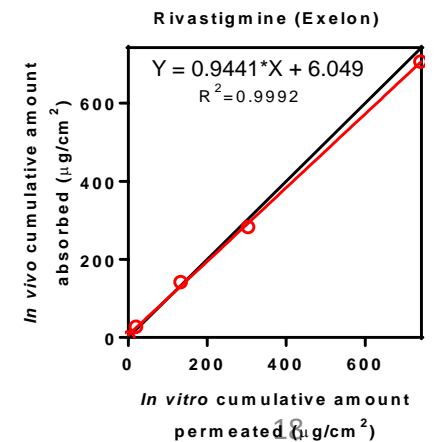
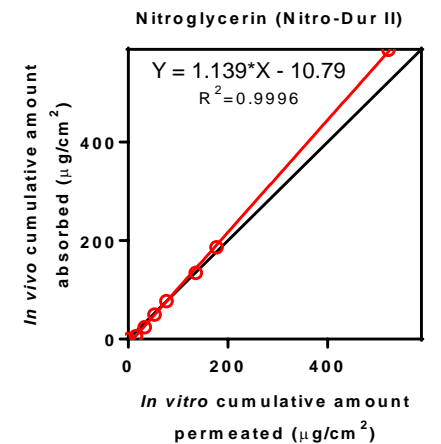
A. *In vitro* skin permeation test (IVPT)



B. 1 stage IVIVR, IVPT convoluted with intravenous pharmacokinetics to predict plasma levels for dose form.



C. 2 stage IVIVR, 1. Deconvolution of plasma data to estimate absorption profiles that are 2. Compared with IVPT data.



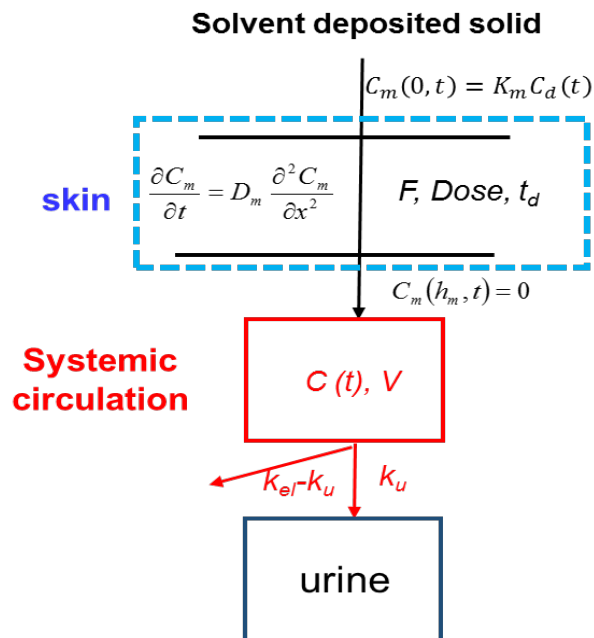


Case study: In practice, we can also model *in vivo* PBPK of topical products applied as a finite dose. Consider the urinary excretion data for 3 drugs in 3 dose forms, courtesy of Tom Franz

Experimental

- Radiolabelled compounds (^{14}C -benzoic acid, ^{14}C -caffeine, ^{14}C -testosterone) were formulated in vehicles: petrolatum, ethylene glycol gel, and water gel
- Formulations were applied to an area of 20-60 cm² using a flat metal spatula to spread a layer of uniform thickness on abdomen.
- Urine was collected throughout the course of experiment until background levels of radioactivity were approached

In vivo PBPK model- Finite dose application, SC diffusion to systemic circulation & excretion into urine



- **Modelling.** 2-stage analysis using a convolution of a finite dose SC diffusion model for skin absorption with a single exponential intravenous disposition phase using Scientist (Micromath) (analysing individual subject data first)

$$\widehat{M}_u(s) = \frac{k_u}{s(s + k_{el})} \frac{F \times dose}{\cosh \sqrt{st_d}}$$

- k_{el} – elimination rate constant (2.37, 0.075, 0.314 h⁻¹ for benzoic acid, caffeine and testosterone, respectively) – obtained from literature data after intravenous dosing
- k_u – urinary elimination rate constant (2.27, 0.055, 0.27 h⁻¹ for benzoic acid, caffeine and testosterone, respectively) – obtained from literature data after intravenous dosing
- F – bioavailability (%) (model parameter)
- t_d – diffusion time (h) (model parameter)

Urinary excretion of benzoic acid, caffeine & testosterone for 3 topical dose forms

First part of 2- stage PBPK analysis using diffusion model

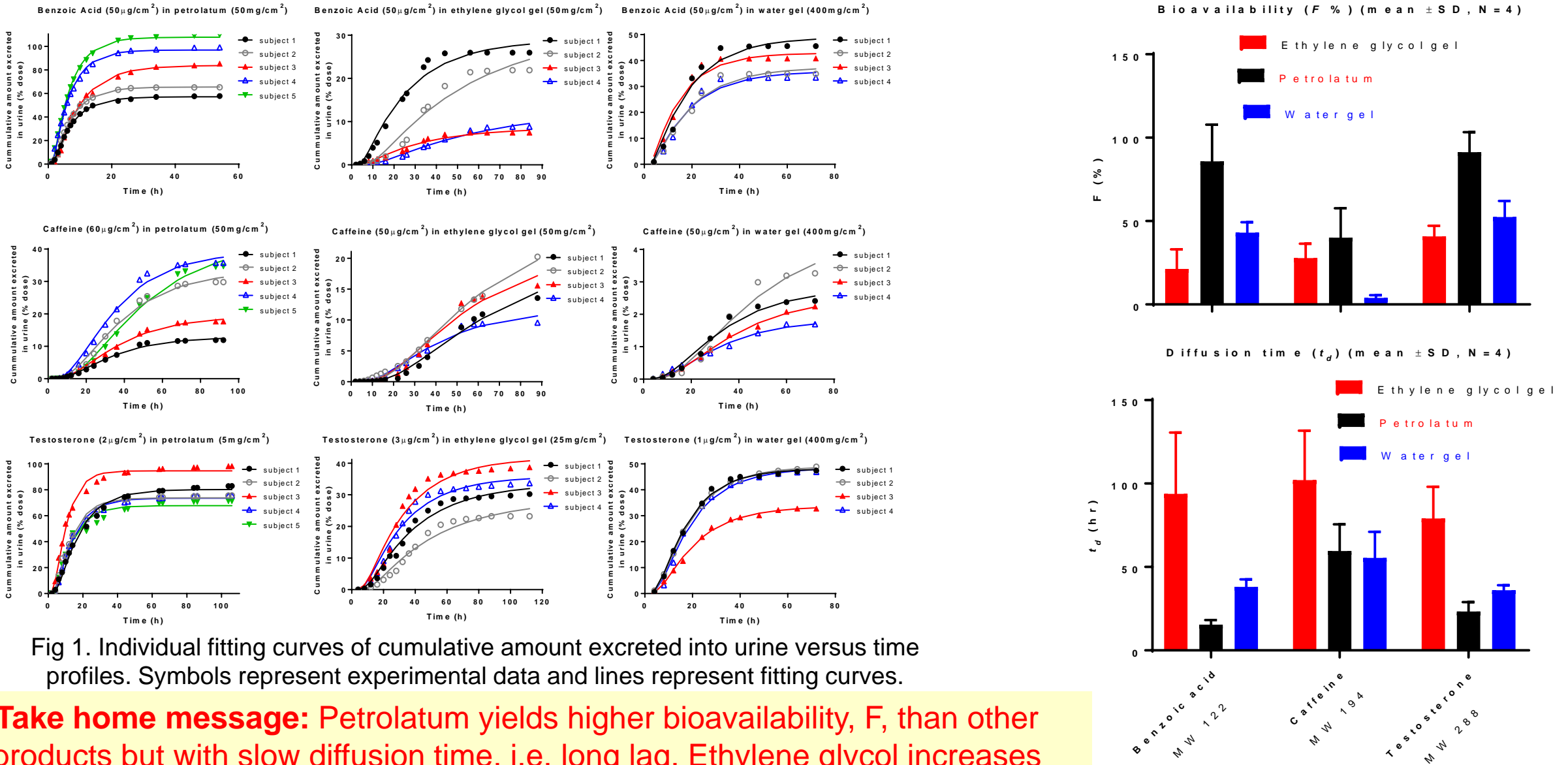
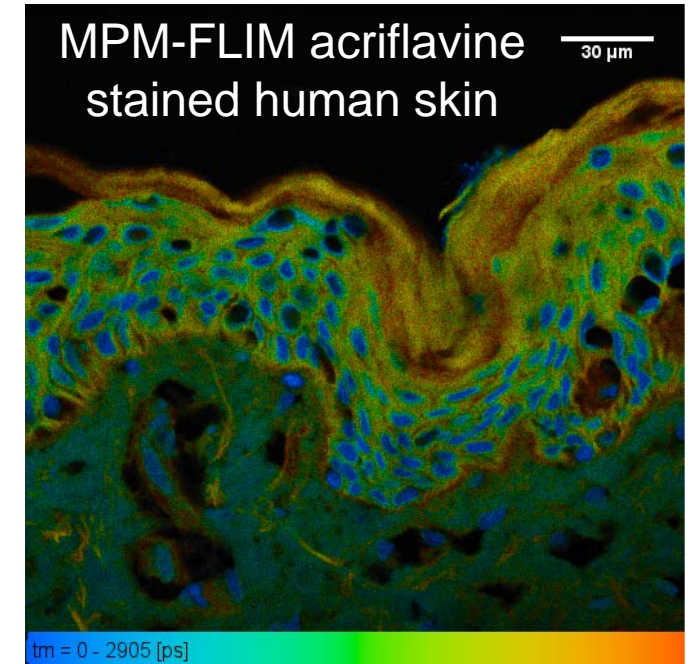


Fig 1. Individual fitting curves of cumulative amount excreted into urine versus time profiles. Symbols represent experimental data and lines represent fitting curves.

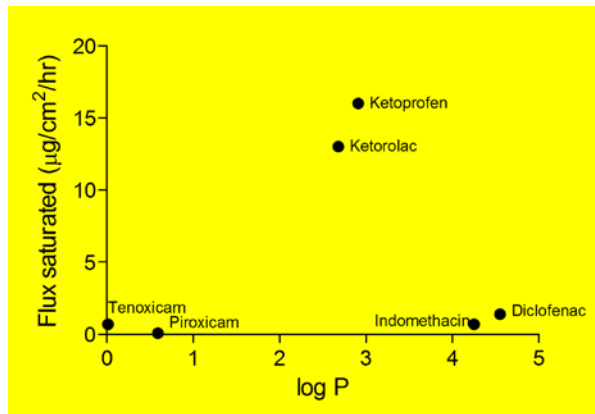
Take home message: Petrolatum yields higher bioavailability, F , than other products but with slow diffusion time, i.e. long lag. Ethylene glycol increases diffusion time with poor $F\%$. Suspect $F\%$ results reflect “like-dissolves-like”

I now want to turn to the mathematical modelling of topical products

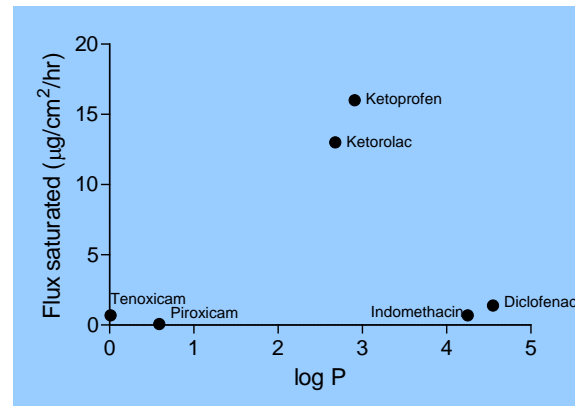
- General principles – we need to aim for a target site of action concentration $C_{SS,L}$ at a local site, e.g. in melanosomes, Langerhan cells, basal keratinocytes, stem cells, sebaceous glands, papillae etc
- If efficacy is not known, it has to be defined by an *in vitro* response – concentration relationships & known absorption rates



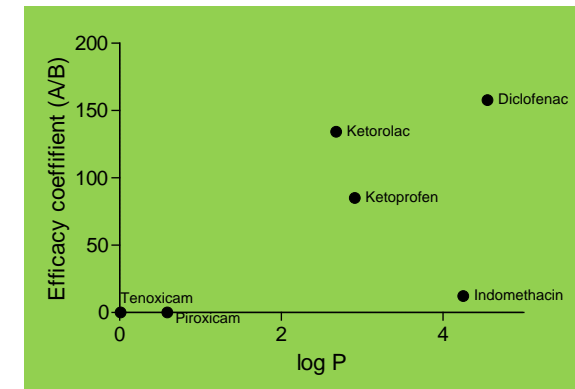
***In vitro* anti-inflammatory minimum inhibitory concentrations for NSAIDs**



Observed skin penetration rates



Efficacy coefficient = penetration X potency



But, model is limited in that it ignores clearance from the putative target site

The concentration at this local site $C_{ss,L}$ is dependent on both rate of delivery to the site & CL_L

$$C_{ss,L} \sim \frac{\text{Rate in. } A}{CL_L}$$

For completeness, this is an approximation and only applies when the clearance is much greater than any back diffusion from the site. The full equation

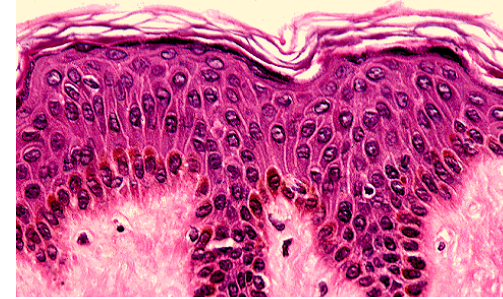
- $C_{ss,L} = \frac{\text{Rate in}}{\frac{CL_L + \frac{K_{sc} D_{sc}}{A}}{K_{ve} h_{sc}}}$ reduces to this simple equation when the clearance term \gg diffusion term.
- At the other extreme of minimal clearance, $C_{ss,L}$ approximate the donor concentration $C_d \cdot K_{ve}$.

Where Rate in= steady state flux per unit area

CL_L is clearance from skin site of action/unit area

$\frac{K_{sc} D_{sc}}{K_{ve} h_{sc}}$ allows for back partitioning at site when there is poor

clearance as would occur with steroid vasoconstriction



In contrast, a similar looking equation applied to systemic blood levels

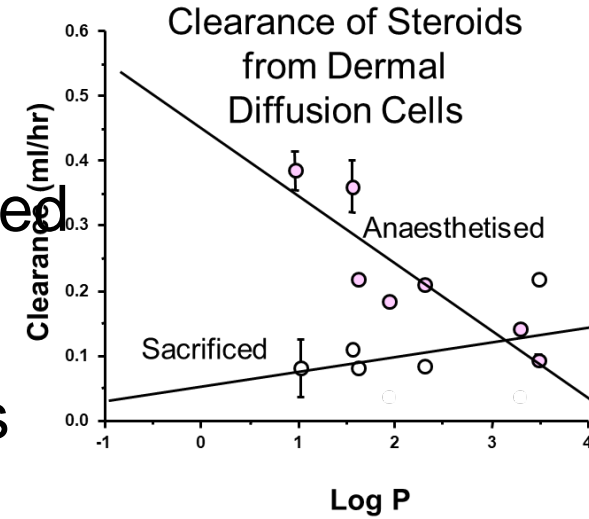
$$C_{ss} \sim \frac{\text{Rate in. } A}{CL}$$

The difference here is that clearance is mainly due to liver metabolism and renal excretion and the rate in is defined by the slowest process – diffusion across the epidermis (including the SC), which is usually much slower than removal by the dermis

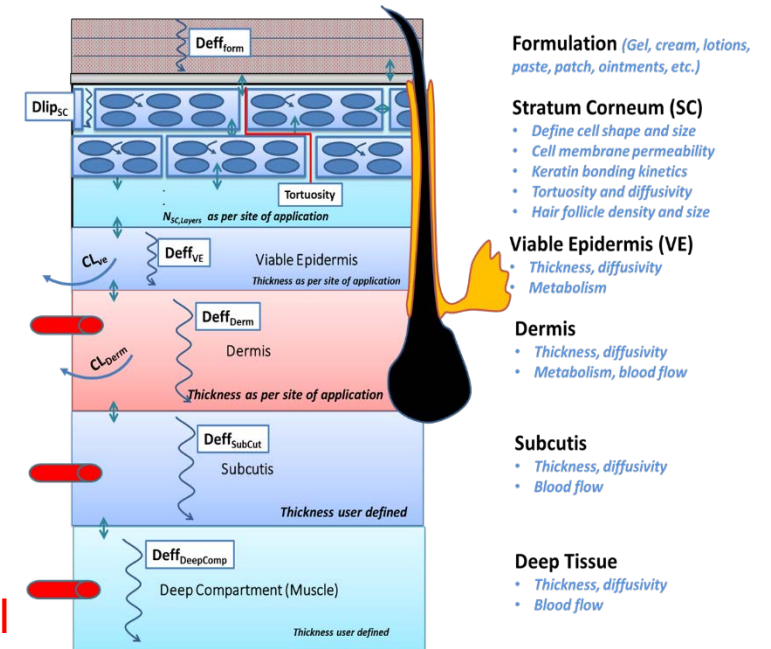
Generally, we do not have this clearance & we have to estimate it

Three approaches.

- **Experimentally** measure the loss of a solute injected at the target site or its appearance in the blood over time, e.g. dermal clearance of cortisol. Or, use a dermal cell applied to skin where the epidermis has been removed
- **Model the clearance** by combining the transfer across the epidermal-dermal junction, diffusion in the dermis above the papillae, transport across the papillae wall & removal by the blood supply to the systemic circulation based on the physicochemical properties of the solute & related physiology
- **Estimate it** from a knowledge of absorption rate & observed concentrations



Note that blood flow (probably due to protein binding) is a major determinant of steroid clearance



We can also estimate $C_{ss,L}$ as an effect response

$$C_{ss,L} \sim \frac{\text{Rate in. A}}{CL_L}$$

One elegant example on $C_{ss,L}$ is the work of WI Higuchi's group on the use of acyclovir to treat herpes virus 1 infections in an *in vivo* animal model

They then deduced

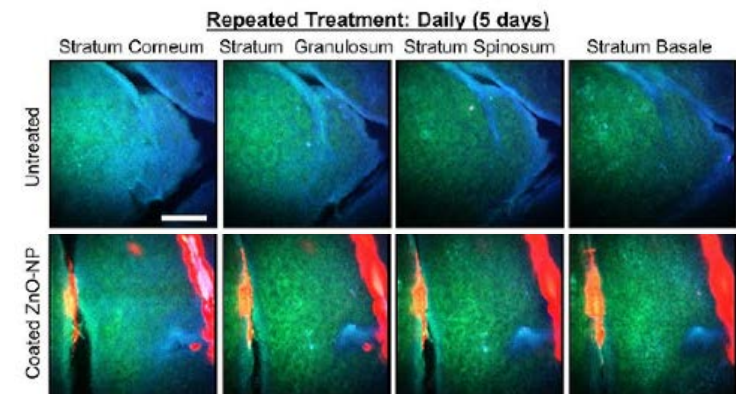
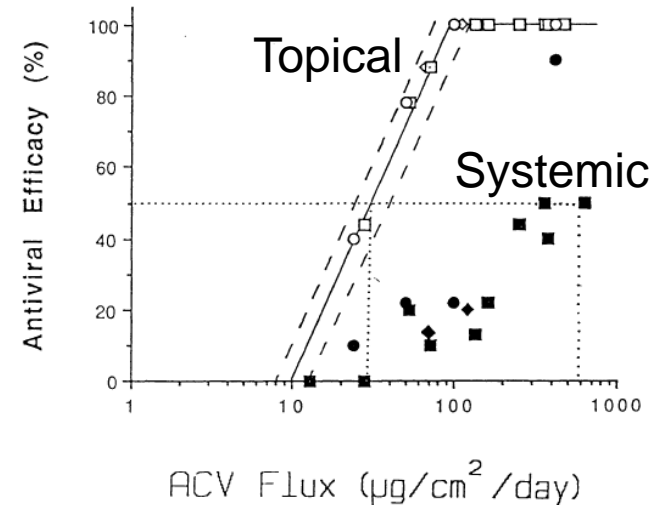
$$\begin{aligned} \text{Topical}_{EC50} &\sim \frac{\text{Topical Rate giving 50\% kill}}{\text{in vivo permeability coefficient for sub papillary de}} \\ &= \frac{30 \frac{\mu\text{g}}{\text{cm}^2} / \text{day}}{1.4 \times 10^{-3} \text{cm/sec}} = 0.25 \mu\text{g/mL} \end{aligned}$$

Similar to *in vivo* blood & *in vitro* cell culture efficacies

Imanindis et al Pharm Res 11(7): 1034-41 (1994)

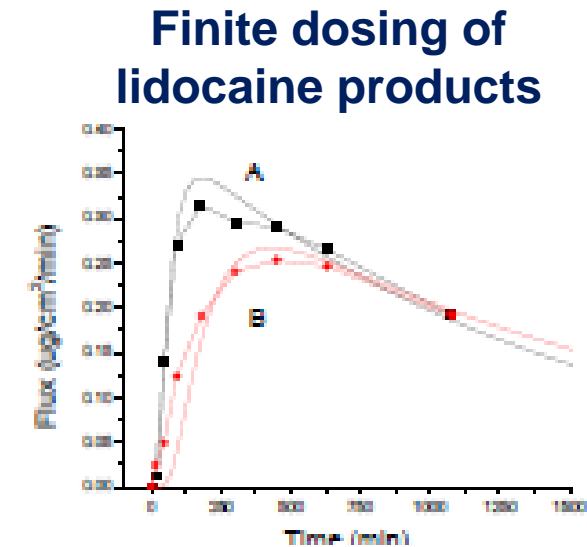
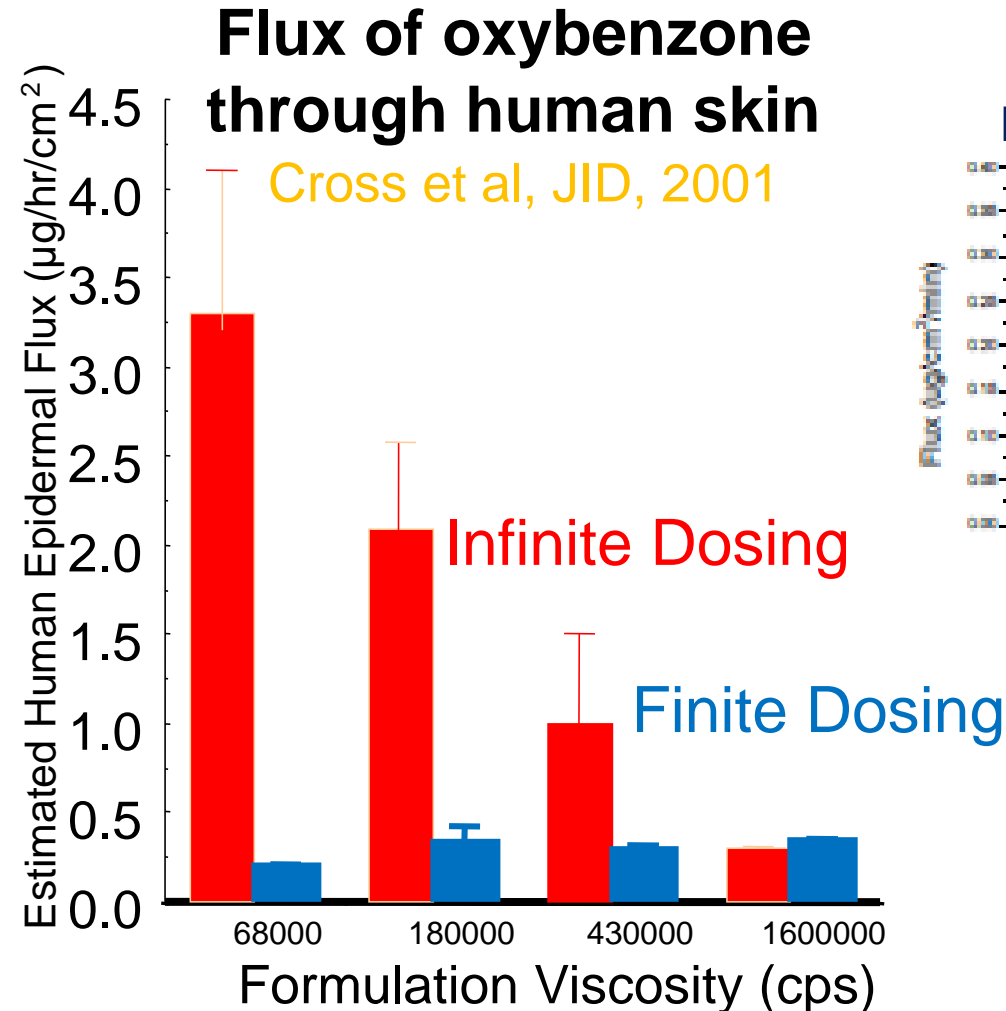
In principle, can then evaluate efficacy of other creams & ointments with this delivery rate

Today, we & others are using changes in individual skin cells' autofluorescence to quantify their response to applied exogenous solutes as we can be imaged *in vivo* non invasively down to about 200 μm below the surface with high resolution. NAD(P)H fluorescence lifetime imaging changes, for instance, define the keratinocyte redox state.



Let us now return to modelling of the absorption of topical products

- Most of the literature has been concerned with infinite dosing.
- There are major dangers in extrapolating to finite dosing, which is how products are applied.
- Lehman (2014) points out that infinite dose study design has proven problematic as the *stratum corneum* is often damaged, saturated, or modified by the continuous exposure to the dosing vehicle.
- He has also shown that when the vehicle is relatively inert, IVPT finite dose modelling is relatively straightforward.

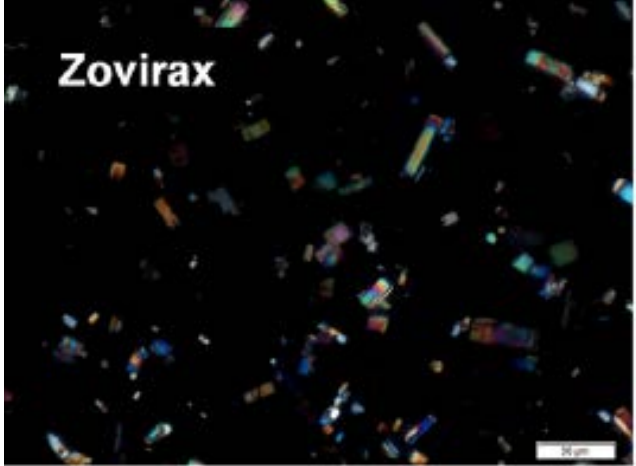
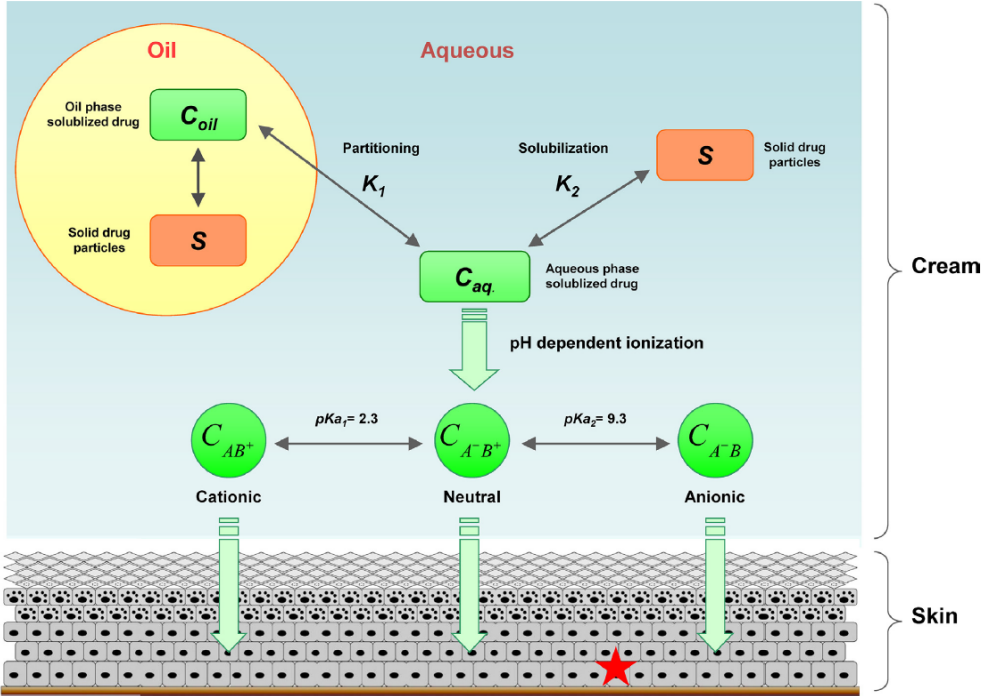


In vitro finite dose percutaneous absorption data (symbols) with overlaid model fit (solid line) for different products. (Lehmann, 2014)

Modelling the complexities of formulation changes after application of finite doses

Consider what happens with Zovirax cream

Complex vehicle



Polarized light microscopy images of various acyclovir cream formulations (200 magnification, bar= 50 μm).

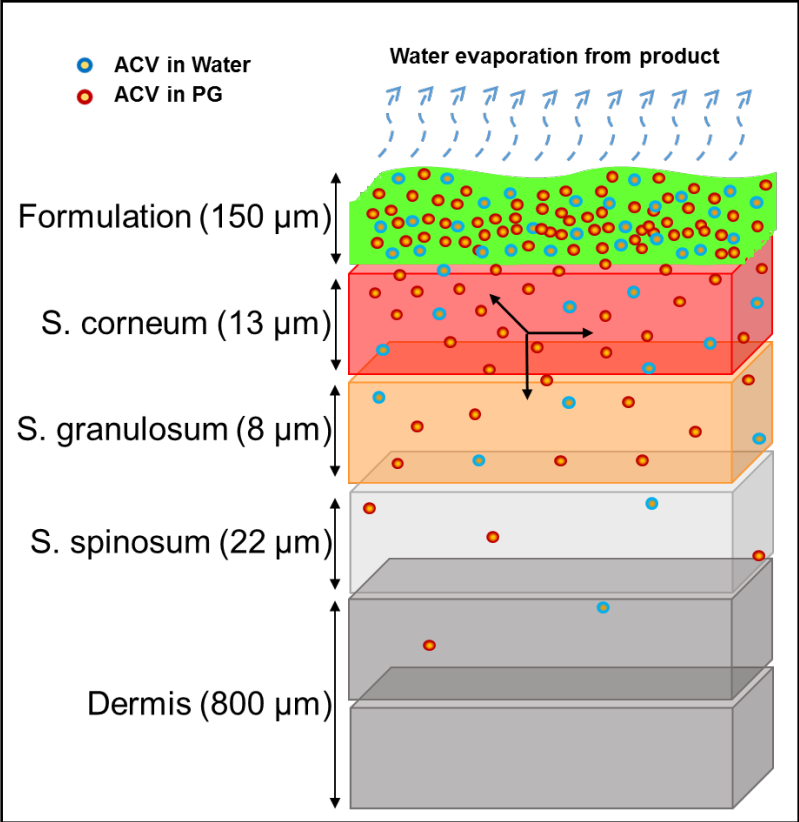
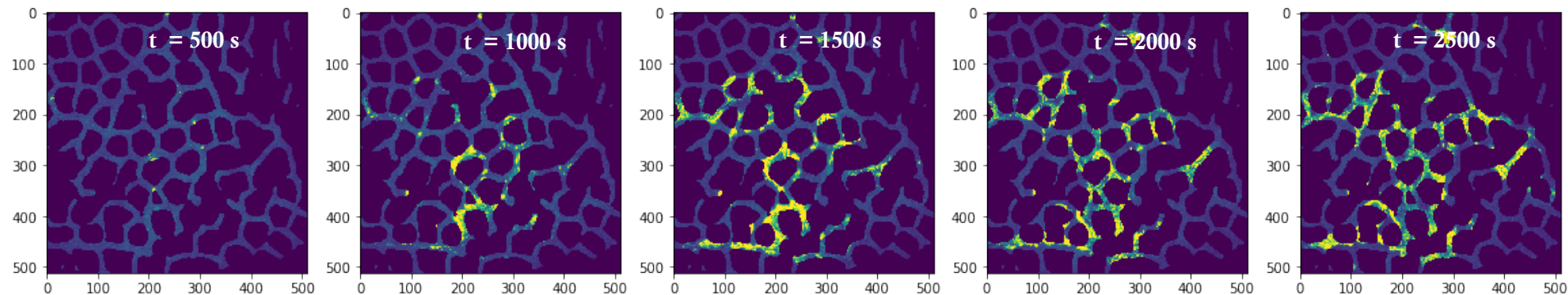
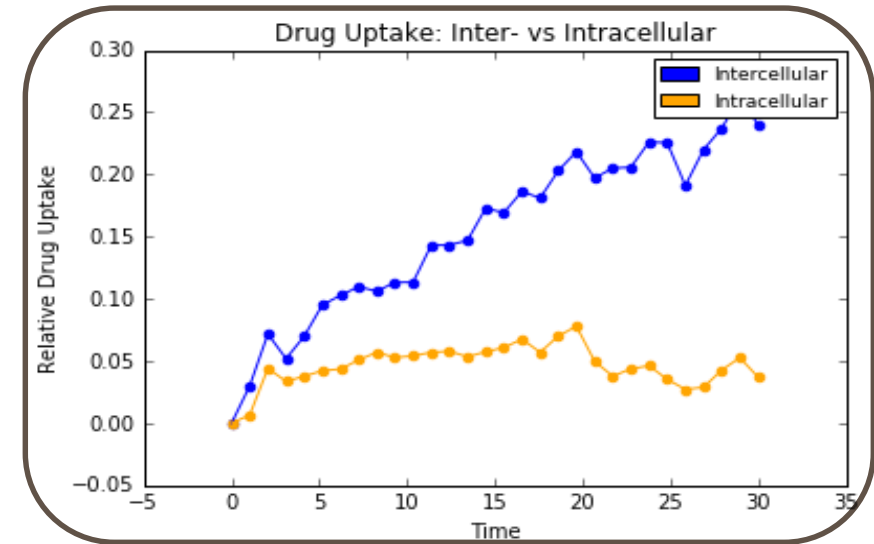
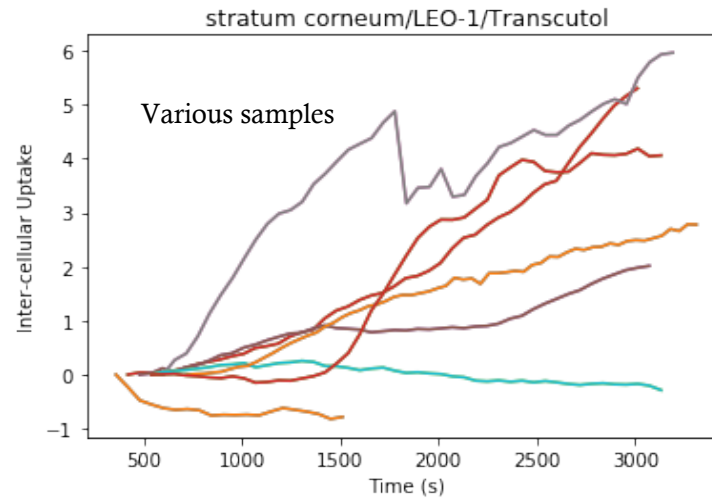
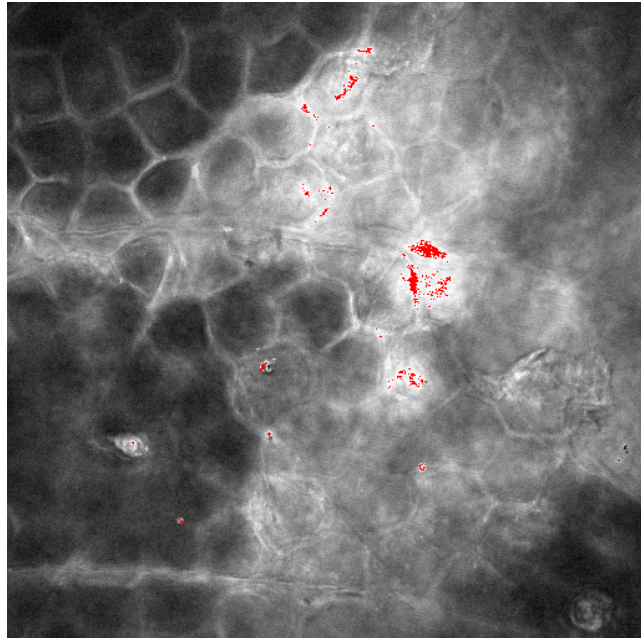


Fig. 2. Role of drug partitioning/solubilization and pH on skin permeation and retention in epidermis from acyclovir cream formulations.

And also depends on mechanisms of skin transport possibly mainly via SC lipids as per Connor Evan's Raman imaging transport of ruxolitinib in Transcutol

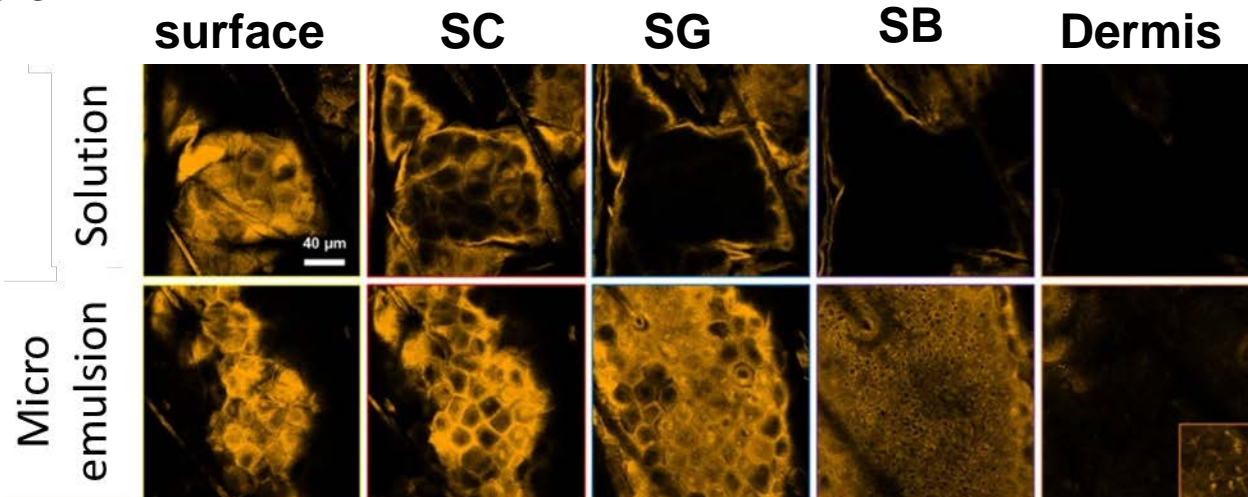
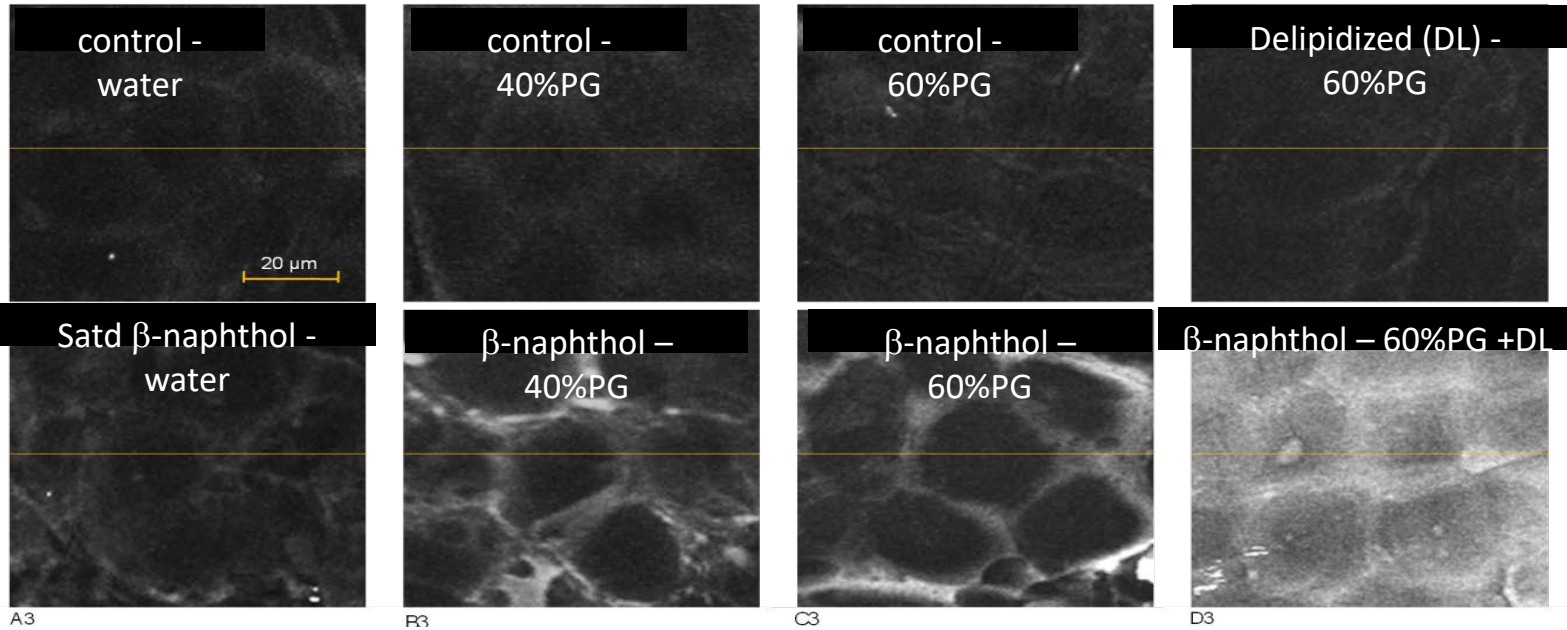


Whilst our MPM data supports Connor's conclusions, there are provisos – the formulation & nature of skin may matter!

Human stratum corneum (SC)

Zhang et al. *J Control Rel* (2011) **154** 50–57

Rose Bengal products applied to ~ 2.5 mm melanoma lesion

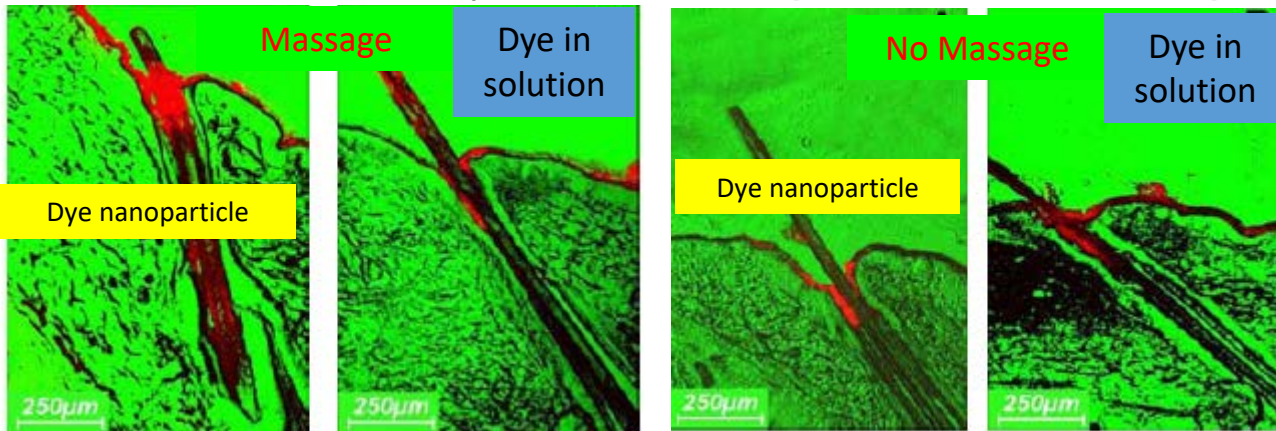


- We have a lot to learn about how formulations affect SC permeability & underlying skin
- A key part of future physiologically based PKPB modelling must be the impact of the various types of skin – site, disease, climate, age etc

Lastly, there may be other pathways that matter

Appendageal & polar pathway a long history of rapid effects

- **Shelley and Melton (1949)** observed perifollicular wheals 5 min after the application of 10 % histamine free base in water.
- Histologic studies by **Mackee et al. (1945)** have also demonstrated follicular diffusion occurring within 5 min.
- Formulation will really matter in depth of follicular deposition

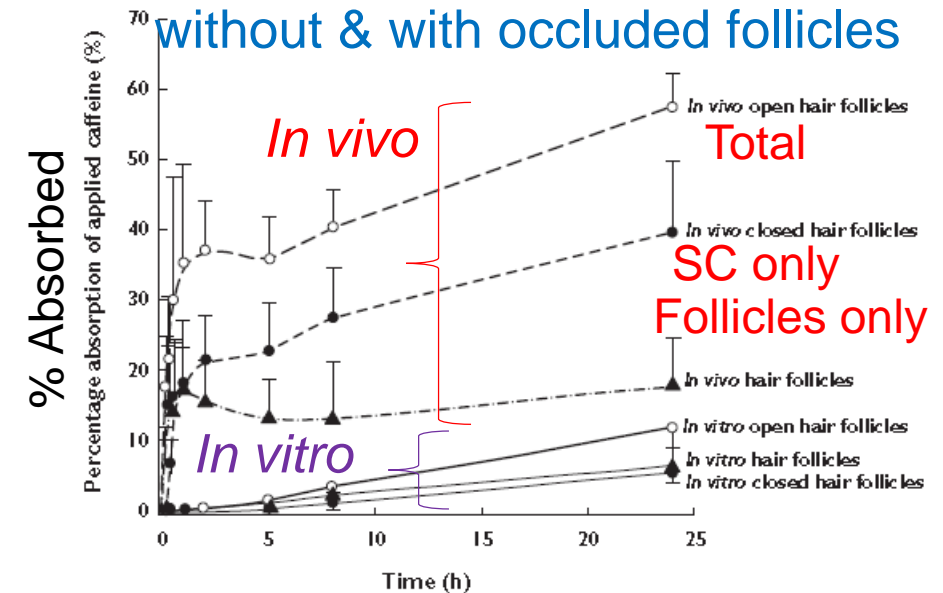


- Viable epidermis & dermis can also matter

- ❖ Significant barriers for more lipophilic solutes
- ❖ Viable epidermal metabolism
- ❖ Diffusion, carriage away by blood supply & shunting to deeper tissues for highly plasma protein bound drugs

Our data with open & closed appendages *in vivo* also suggests it occurs at early times for solvent deposited solids & >> *in vitro*

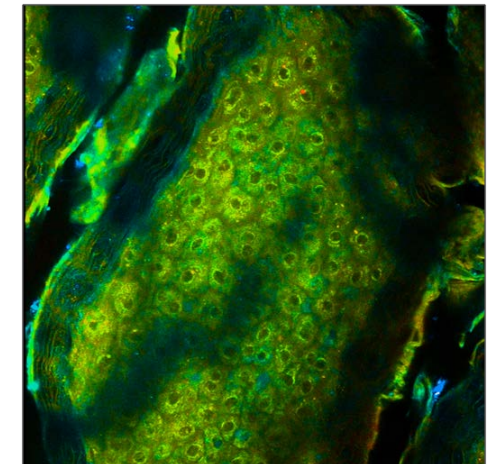
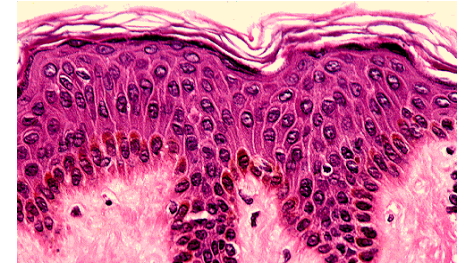
Human *in vivo* and *in vitro* after solvent deposited solid of caffeine without & with occluded follicles



Liu et al *Br J Clin Pharmacol*
2011; 72: 768–774

Conclusion

- The mathematical modelling of skin transport is relatively straightforward in assessing transdermal delivery
- However, it is not so straightforward for topical delivery where it is difficult to measure both the target site concentrations of actives & local clearance from the site
- Our future will very much depend on us using a combination of mechanistic predictions and observation – the middle out approach.
- Thank you for listening



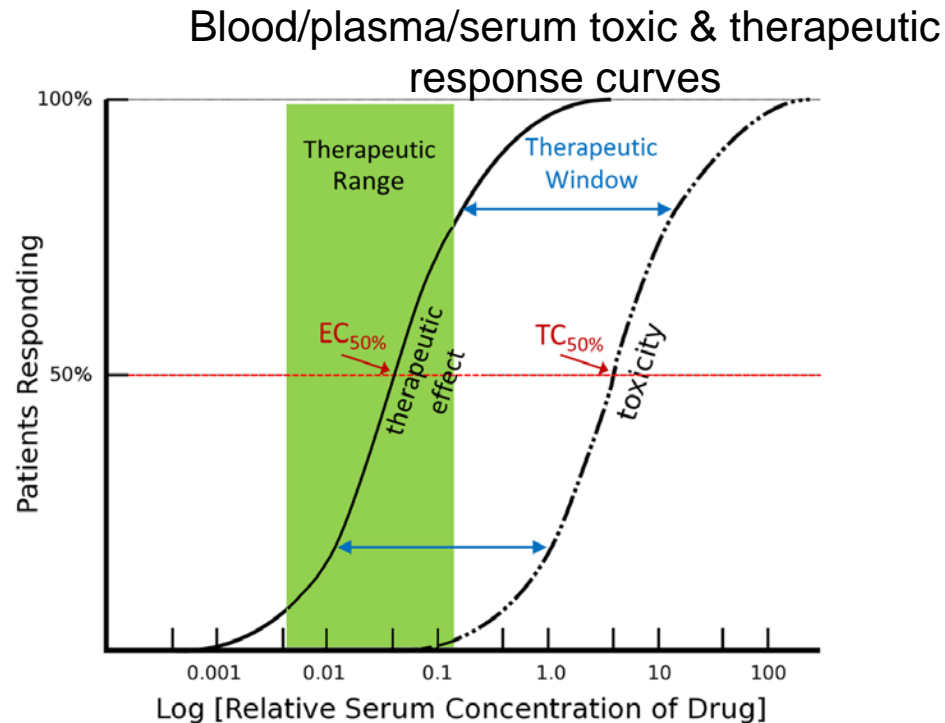
The views expressed in this presentation are mine alone and do not reflect the official policies of the Food and Drug Administration, or the Department of Health and Human Services; nor does any mention of trade names, commercial practices, or organization imply endorsement by the United States Government.

Efficacy & safety of transdermal & topical products

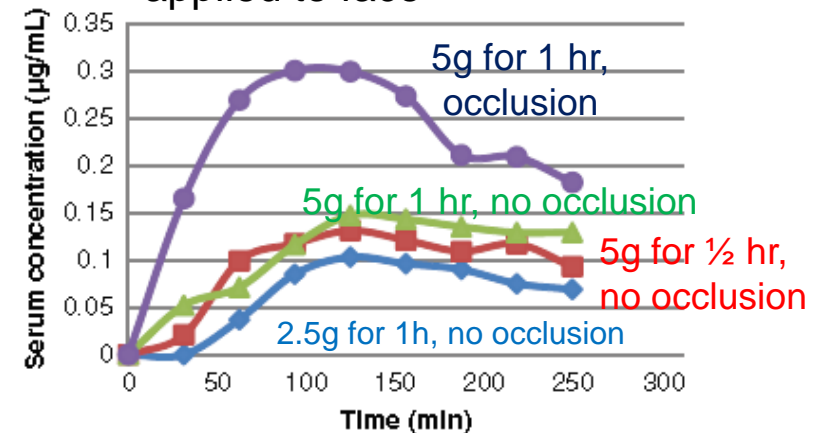
Mathematical models can define C_{ss} from desired therapeutic effect, maximum response, EC_{50} & time to effect. Individual PBPK defining dosing regimen is then used to achieve C_{ss}

<http://holford.fmhs.auckland.ac.nz/docs/immediate-time-course-of-drug-effect.pdf> 2019

- **Transdermal products C_{ss} must be within the Therapeutic Range**
- **Topical products systemic plasma concentrations should be less than the Therapeutic Range to not cause any unwanted systemic effects**



Lidocaine 4% topical anesthetic cream (LMX 4, Ferndale Laboratories, MI) applied to face



< Lower lidocaine therapeutic concentration of $1\mu\text{g/mL}$ for symptomatic dysrhythmias.

Oni Aesthetic Surg J 30(6) 853–858, 2010

“Systemic absorption of topical corticosteroids can produce reversible hypothalamic-pituitary-adrenal (HPA) axis suppression with the potential for glucocorticosteroid insufficiency after withdrawal of treatment.”

https://www.galderma.com/sites/g/files/jcdfhc196/files/inline-files/Clobex%20Shampoo%20PM_E_Jan.%202006%2C%202020.pdf