



# Stochastic and Deterministic Analysis of Reactivity Ratios in the Partially Reversible Copolymerization of Lactide and Glycolide

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**Louise Kuehster**, Young Kuk Jhon, Yan Wang, William C. Smith,  
Xiaoming Xu, Bin Qin, Feng Zhang, Nathaniel A. Lynd

November 13, 2022



# Thank you!



Dr. Feng Zhang



Mark Costello

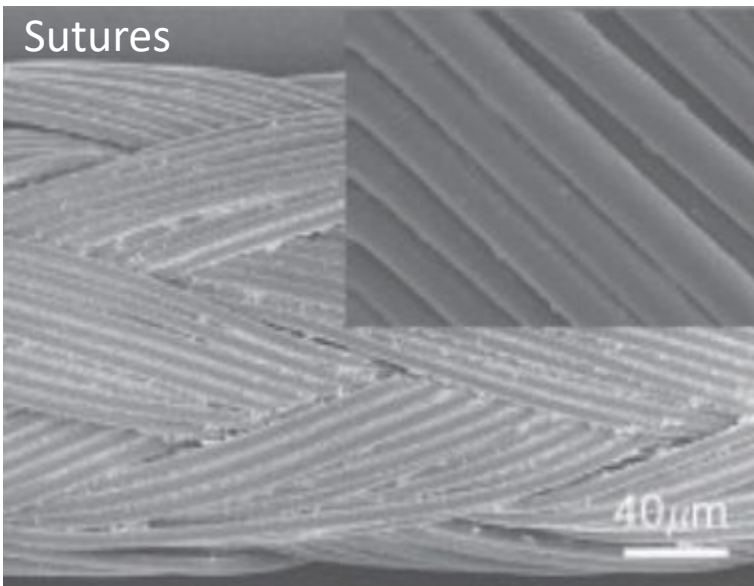
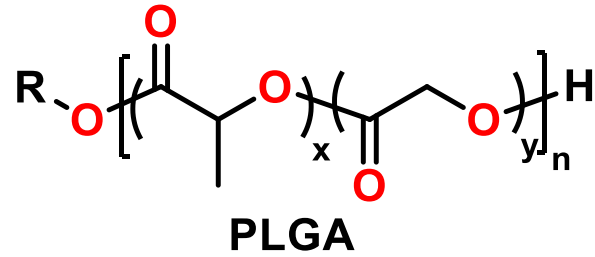


Dr. Beibei Chen

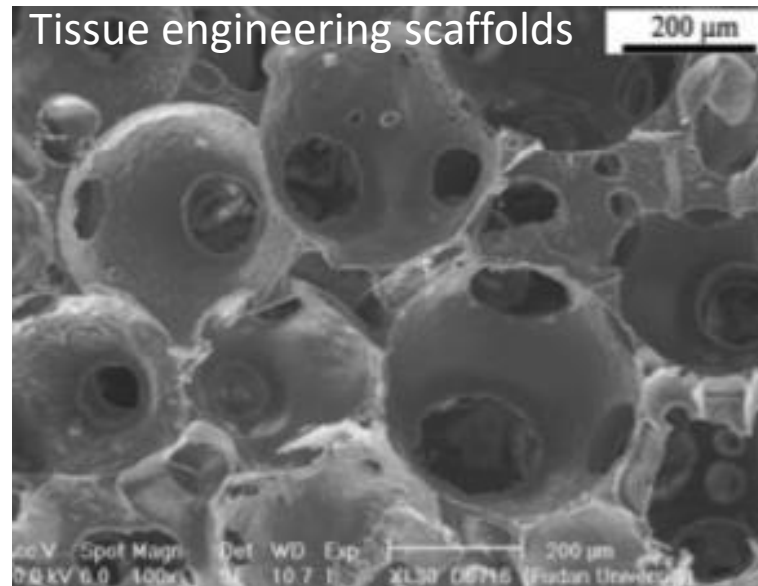




# Poly(lactide-co-glycolide) (PLGA) is a biodegradable polymer that is used in pharmaceutical applications



Antimicrobial and Biodegradable PLGA Medical Sutures with Natural Grapefruit Seed Extracts. *Mater. Lett.* **2013**, 95, 40–43. <https://doi.org/10.1016/j.matlet.2012.12.090>.

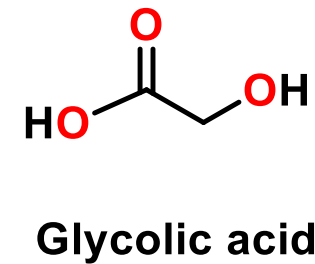
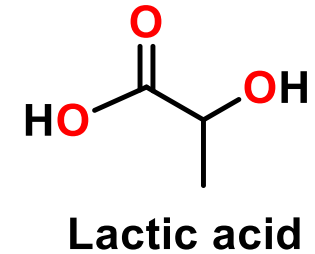
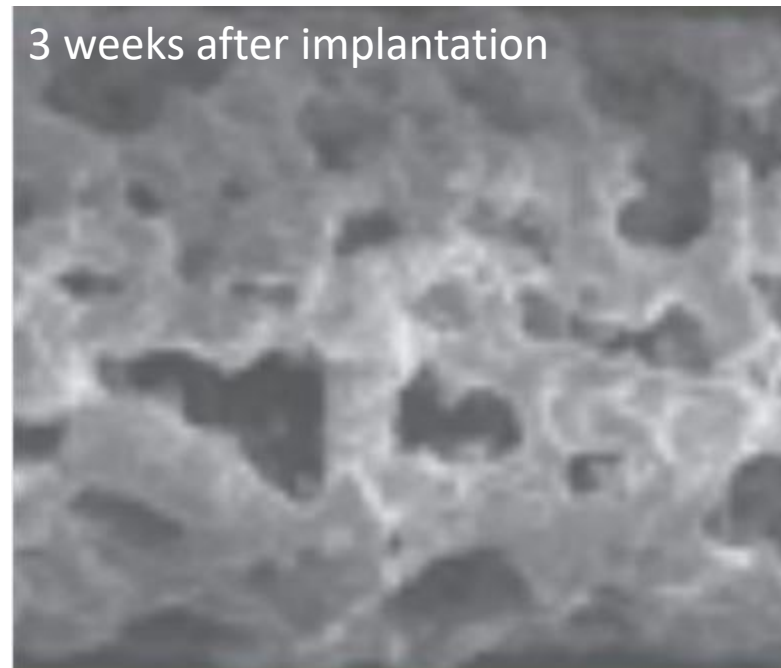
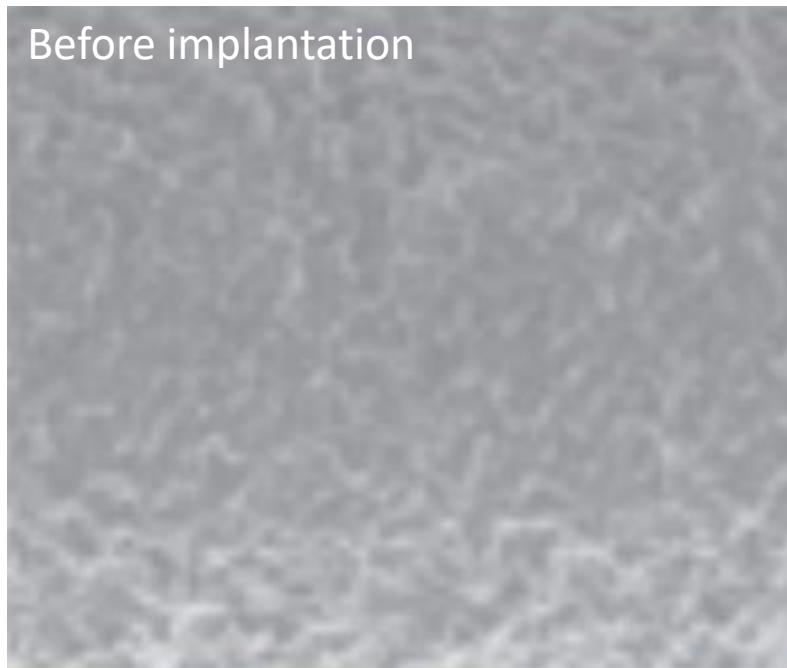
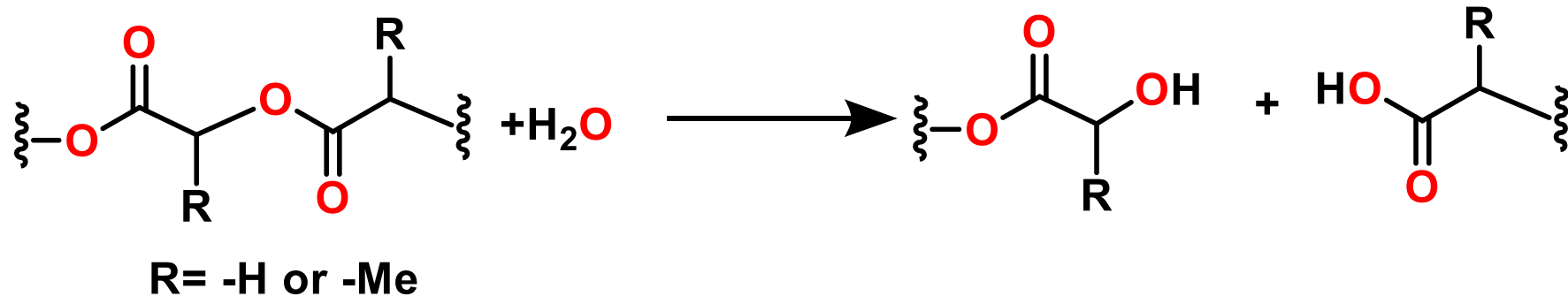


Junchuan Zhang; Hong Zhang; Linbo Wu; Jiandong Ding. Fabrication of Three Dimensional Polymeric Scaffolds with Spherical Pores. *J. Mater. Sci.* **2006**, 41 (6), 1725–1731. <https://doi.org/10.1007/s10853-006-2873-7>.



OZURDEX® Mechanism of Action | For HCPs <https://hcp.ozurdex.com/mechanism-of-action> (accessed Mar 27, 2021).

# PLGA biodegrades to non-toxic products



OZURDEX® Mechanism of Action | For HCPs <https://hcp.ozurdex.com/mechanism-of-action> (accessed Mar 27, 2021).

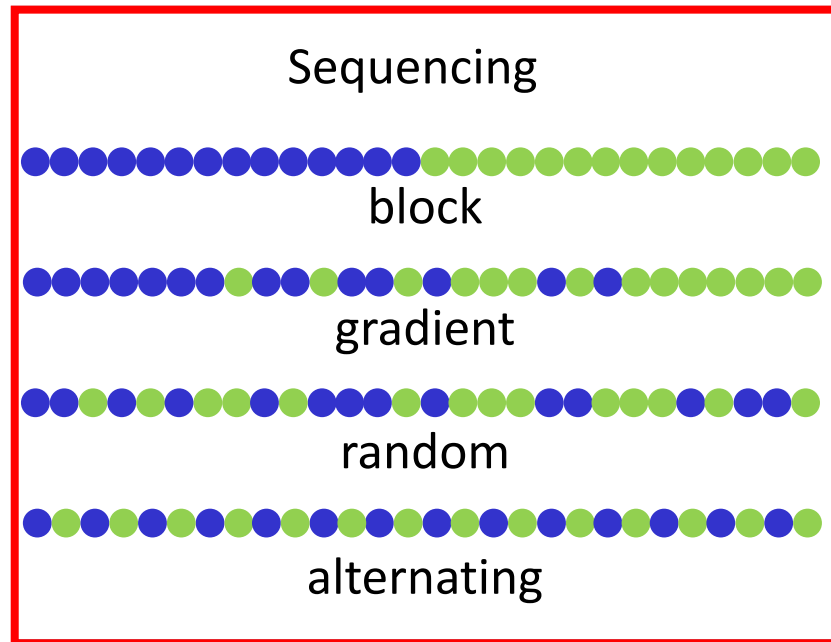
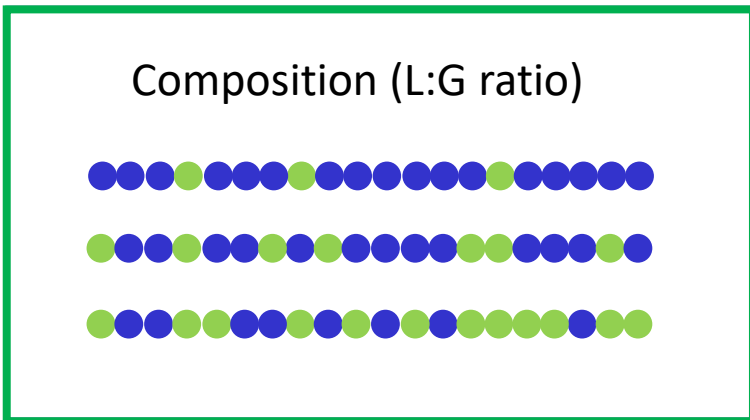
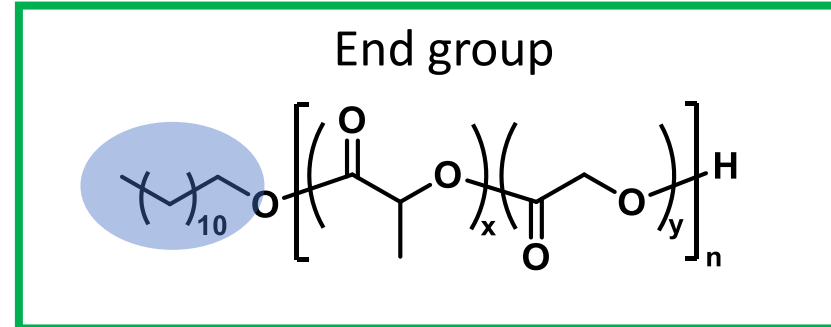
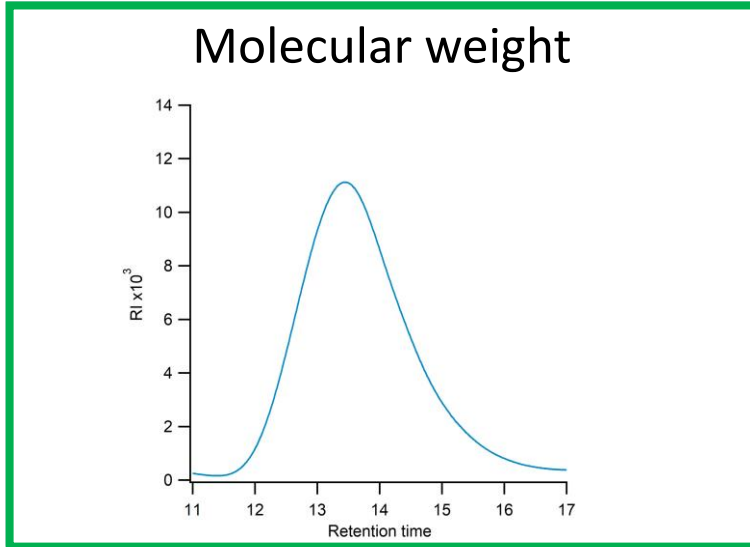
# Long-acting drug implants can improve patient outcomes



- Lower dosage frequency
- Better patient compliance
- Potentially lower drug toxicity

There are over 20 FDA-approved products which use PLGA as an excipient, but no generic version have been approved

# Multiple characteristics affect PLGA degradation and drug release



Understanding sequencing will expand PLGA's usefulness as an excipient

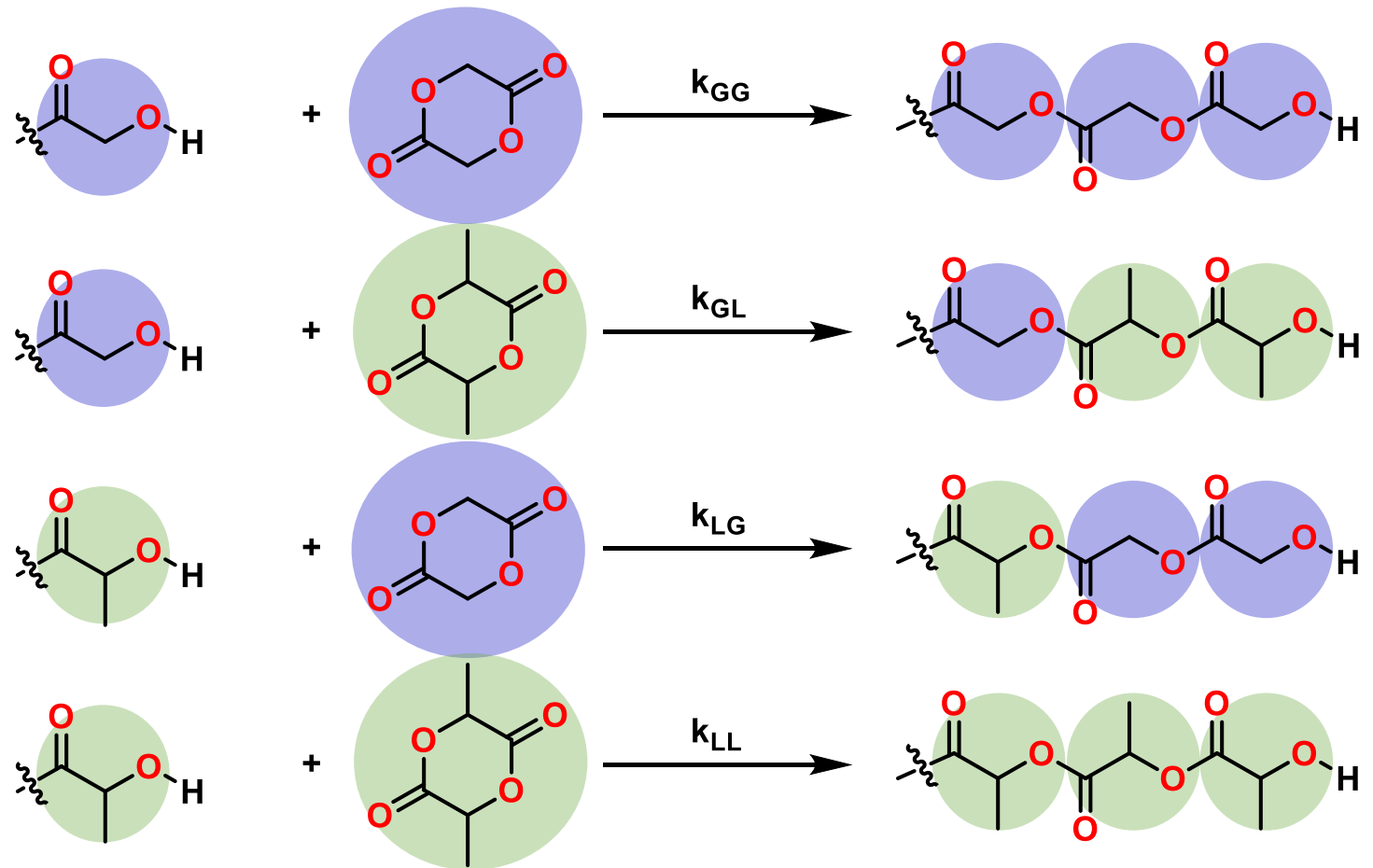
- Enable better design of new PLGA products
- Improve the FDA's ability to regulate current PLGA products

← Not easily characterized or controlled

# Copolymer sequence is usually understood in terms of reactivity ratios

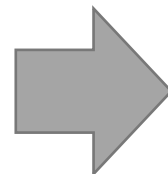
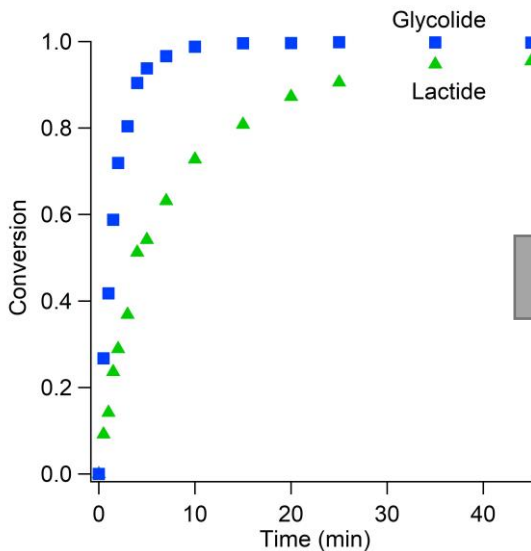
$$r_G = \frac{k_{GG}}{k_{GL}}$$

$$r_L = \frac{k_{LL}}{k_{LG}}$$



# Copolymer sequence is currently understood in terms of reactivity ratios

Kinetic monomer consumption data



Reactivity ratios

$$r_G, r_L \gg 1$$

$$r_G > 1, r_L < 1$$

$$r_G, r_L \approx 1$$

$$r_G, r_L \ll 1$$

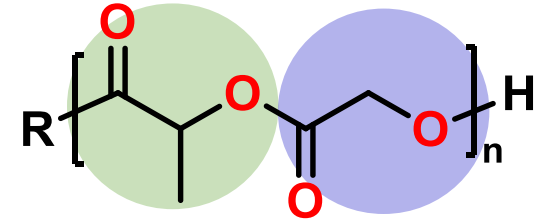
Microstructure

Blocky

Gradient

Random

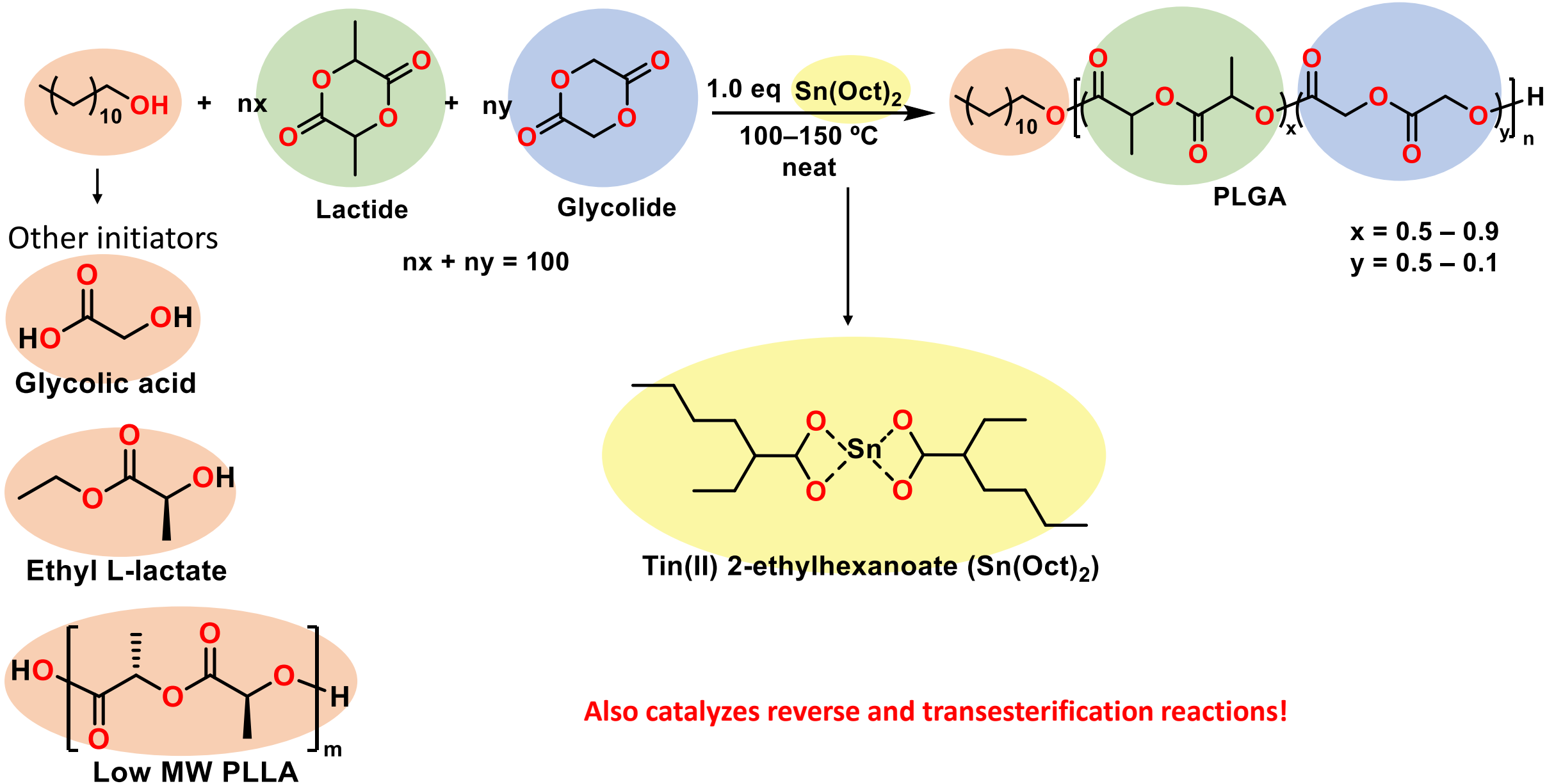
Alternating



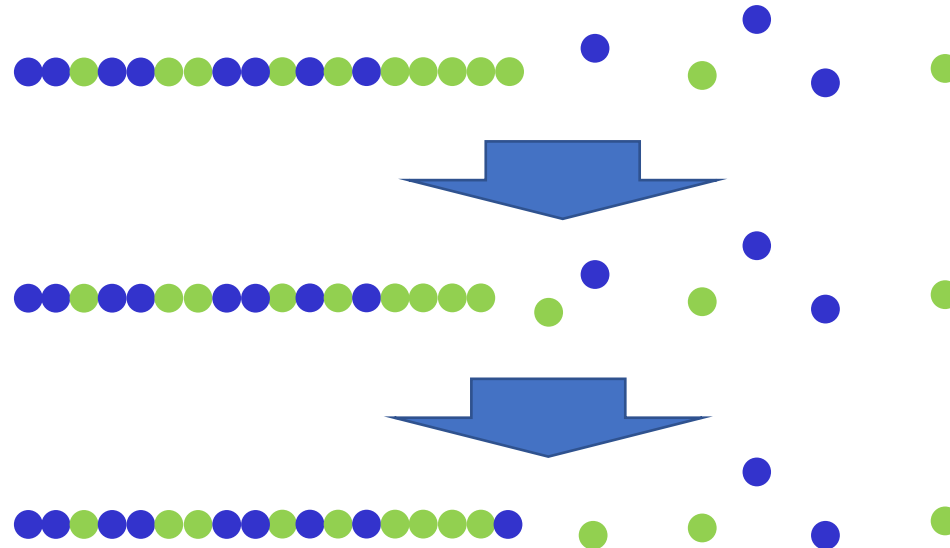
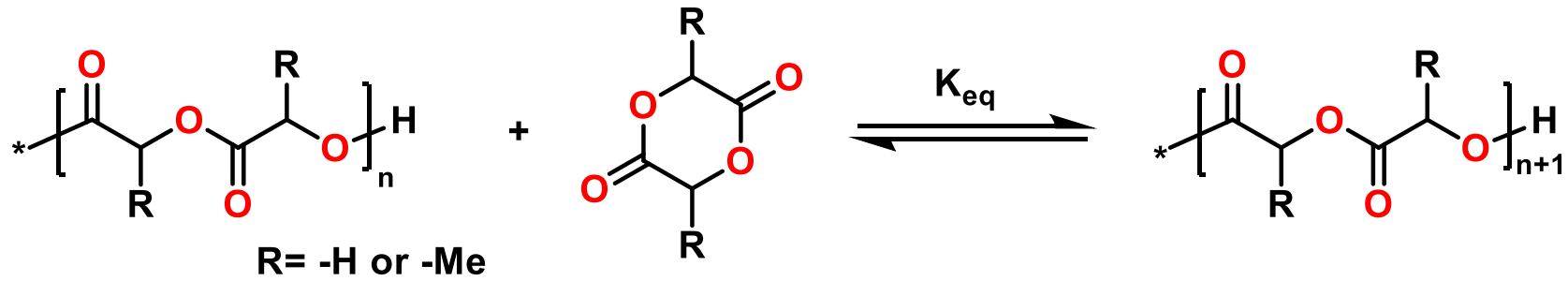
Unfortunately, current models aren't sufficient for PLGA



# PLGA is synthesized from cyclic dimers

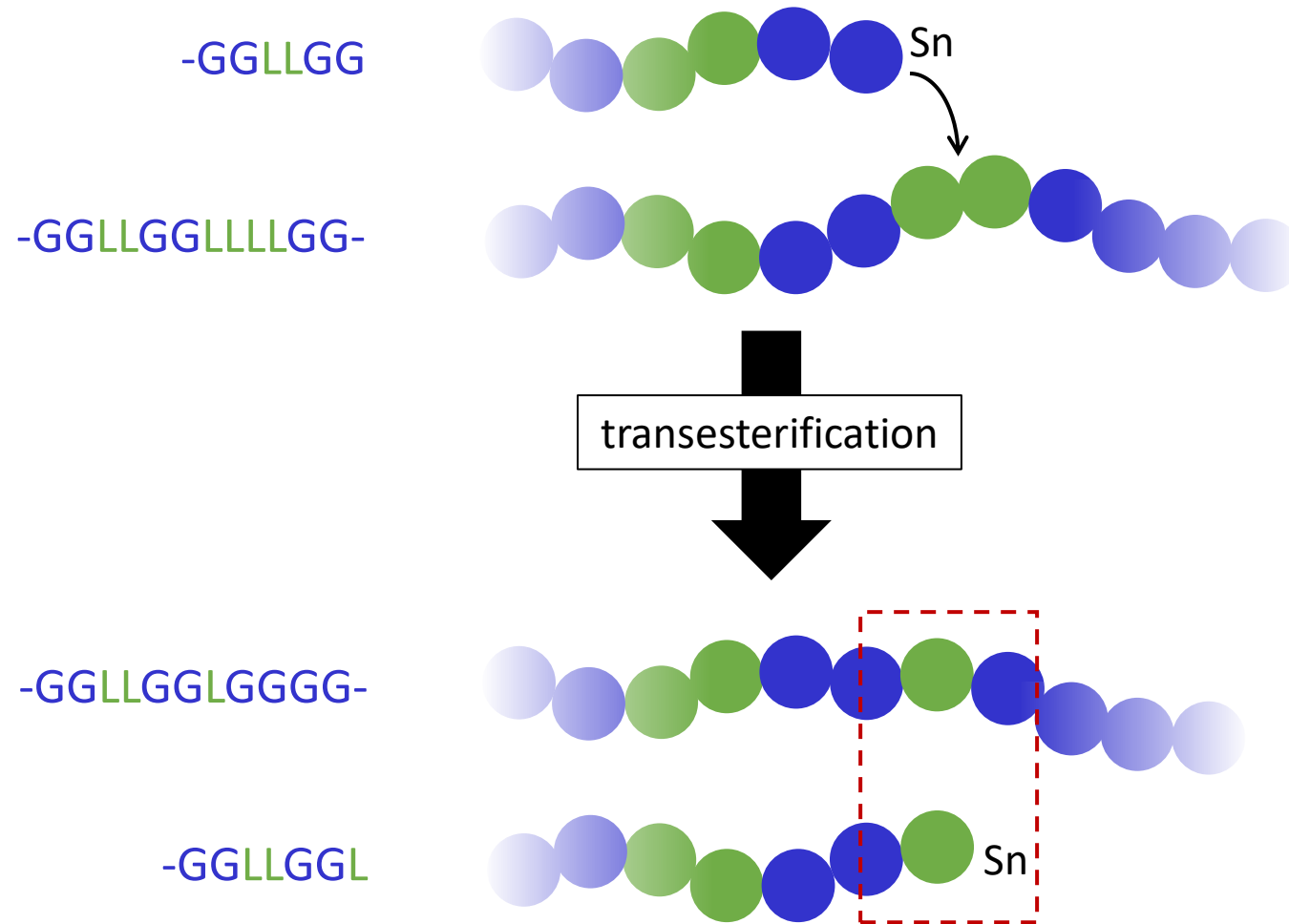


# Sequence is altered throughout the polymerization as a result of equilibrium



These reactions are not accounted for in the equations used to calculate reactivity ratios, so any reactivity ratios we calculate with those models are inaccurate

# Transesterification scrambles sequence throughout synthesis



Even if we calculate accurate reactivity ratios, the sequence is also affected by transesterification

- Calculate accurate reactivity ratios that account for reversibility
- Measure kinetics of transesterification
- Link both to actual sequence through modeling

# Equations describing PLGA copolymerization are complicated

Initiation reactions

$$\begin{aligned} r_1 &= k_G c_G(t) c_I(t) \\ r_2 &= k_L c_L(t) c_I(t) \end{aligned}$$

$$\frac{dc_I}{dt} = -r_1 - r_2$$

Forward polymerization reactions

$$\begin{aligned} r_3 &= k_{GG} c_{P_G}(t) c_G(t) \\ r_4 &= k_{GL} c_{P_G}(t) c_L(t) \\ r_5 &= k_{LG} c_{P_L}(t) c_G(t) \\ r_6 &= k_{LL} c_{P_L}(t) c_L(t) \end{aligned}$$

$$\frac{dc_G}{dt} = -r_1 - r_3 - r_5 + r_7 + r_9$$

$$\frac{dc_L}{dt} = -r_2 - r_4 - r_6 + r_8 + r_{10}$$

Depolymerization reactions

$$\begin{aligned} r_7 &= k_{G-G} c_{P_{GGG}}(t) \\ r_8 &= k_{G-L} c_{P_{GLL}}(t) \\ r_9 &= k_{L-G} c_{P_{LGG}}(t) \\ r_{10} &= k_{L-L} c_{P_{LLL}}(t) \end{aligned}$$

$$\frac{dc_{P_G}}{dt} = r_1 - r_4 + r_5 + r_8 - r_9$$

$$\frac{dc_{P_L}}{dt} = r_2 + r_4 - r_5 - r_8 + r_9$$

Transesterification

$$r_{11} = k_T c_{ends} c_{esters}$$

Because of depolymerization reactions, we need to know the concentration of every possible polymer sequence, which gives  $2^n$  equations ( $n$ =max. degree of polymerization)  
Too many equations to solve



# Two ways we can circumvent mathematical challenges

- Instead of integrating  $2^n$  deterministic equations, solve the problem stochastically
- Make some simplifying assumptions so that there are fewer equations to solve

Divide the interval 0 to 1 according to the probability of each possible reaction (based on rate equations)

Generate a random number between 0 and 1 to select the next reaction that will occur

Generate another random number to choose which molecule will be reacted

Generate a third random number which will be used to update the time according to the Gillespie algorithm,  $t_{n+1} = t_n - \frac{\log(a)}{r_{tot}}$

- Preliminary data shows little glycolide reversibility and fast glycolide consumption → assume only lactide is reversible, and chain ends are always lactide by end of reaction

Initiation reactions

$$\begin{cases} r_1 = k_G c_G(t) c_I(t) \\ r_2 = k_L c_L(t) c_I(t) \end{cases}$$

Forward polymerization reactions

$$\begin{cases} r_3 = k_{GG} c_{P_G}(t) c_G(t) \\ r_4 = k_{GL} c_{P_G}(t) c_L(t) \\ r_5 = k_{LG} c_{P_L}(t) c_G(t) \\ r_6 = k_{LL} c_{P_L}(t) c_L(t) \end{cases}$$

Depolymerization reactions

$$r_{10} = k_{L-L} c_{P_{LLL}}(t)$$

- Valid only for low glycolide composition

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- Instead of integrating  $2^n$  deterministic equations, solve the problem stochastically
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Both models include a third reactivity ratio to represent lactide reversibility

$$r_G = \frac{k_{GG}}{k_{GL}}, \quad r_L = \frac{k_{LL}}{k_{LG}}, \quad r_R = \frac{k_{L-L}}{k_{LL}}$$

composition

$$\left\{ \begin{array}{l} r_1 = k_G c_G(t) c_I(t) \\ r_2 = k_L c_L(t) c_I(t) \end{array} \right.$$

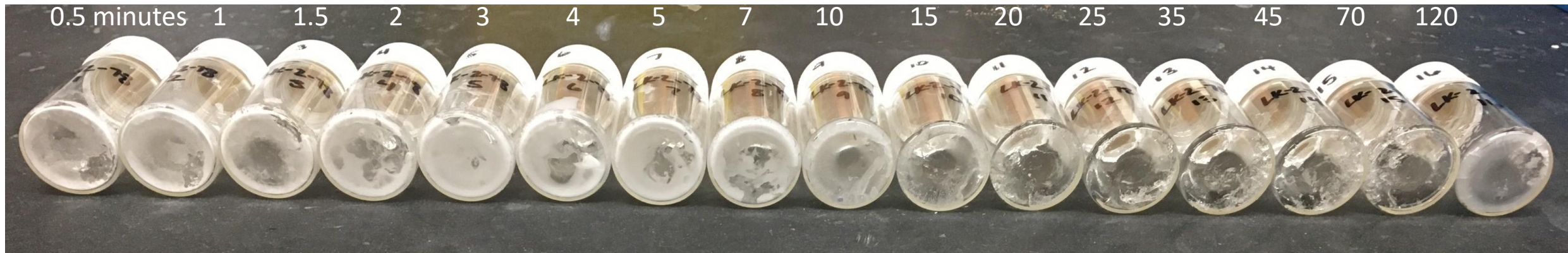
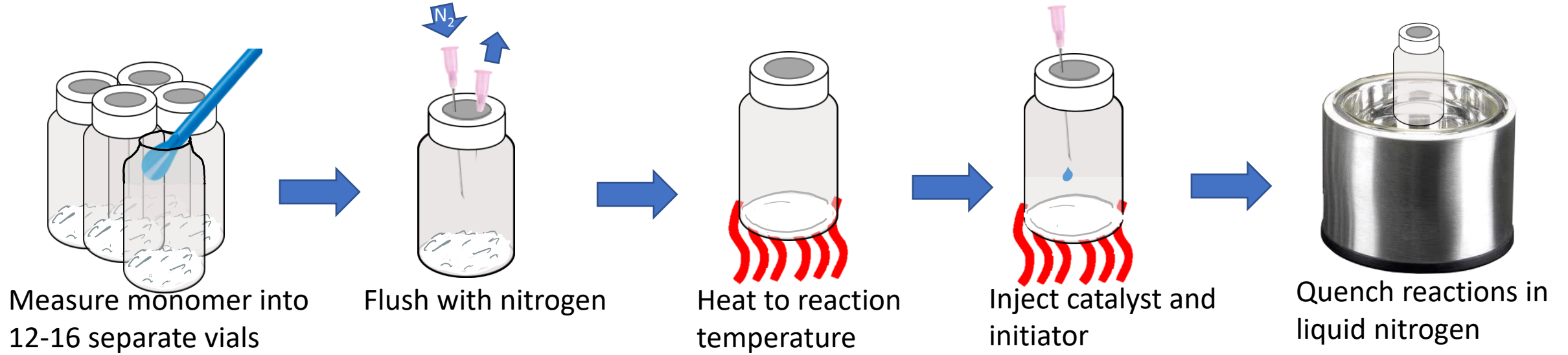
$$\left\{ \begin{array}{l} r_3 = k_{GG} c_{P_G}(t) c_G(t) \\ r_4 = k_{GL} c_{P_G}(t) c_L(t) \\ r_5 = k_{LG} c_{P_L}(t) c_G(t) \\ r_6 = k_{LL} c_{P_L}(t) c_L(t) \end{array} \right.$$

Forward polymerization reactions

Depolymerization reactions

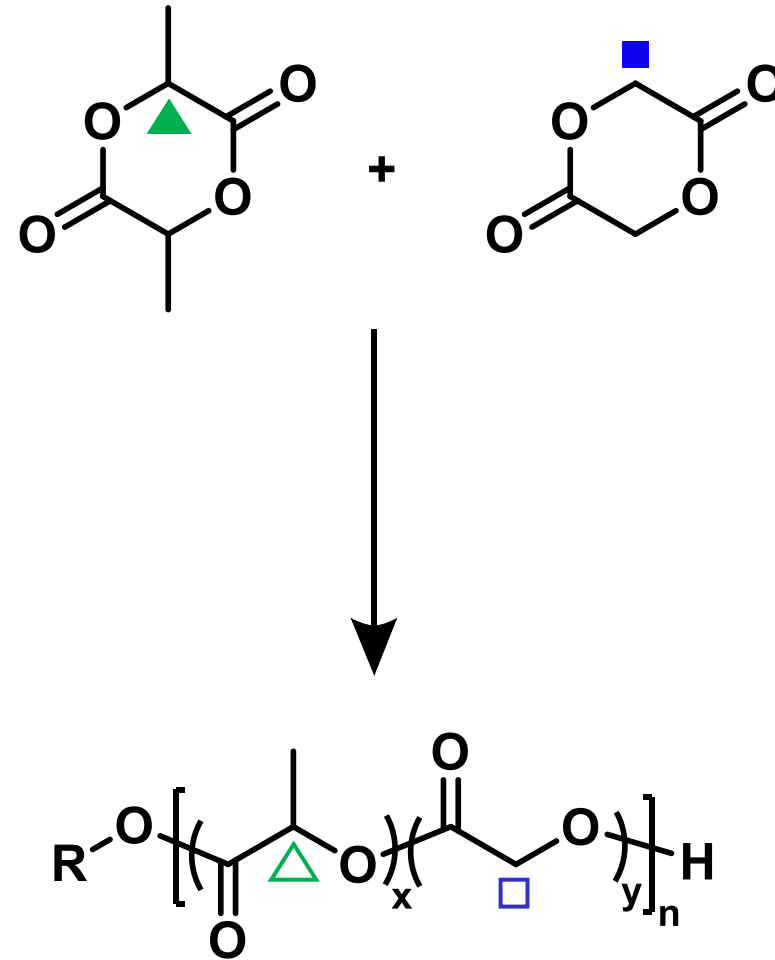
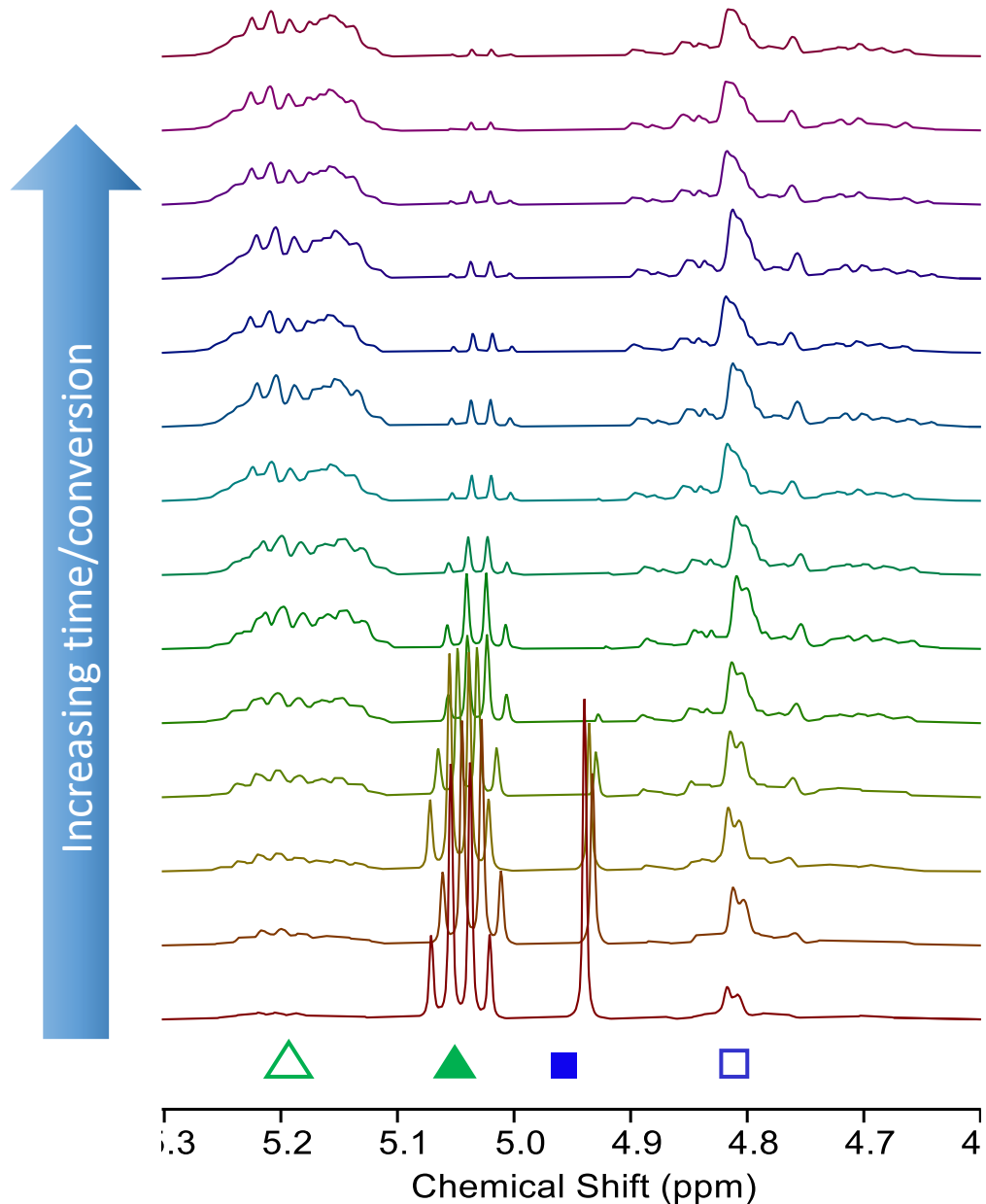
$$\left\{ \begin{array}{l} r_{10} = k_{L-L} c_{P_{LLL}}(t) \end{array} \right.$$

# Kinetic data for PLGA has been collected



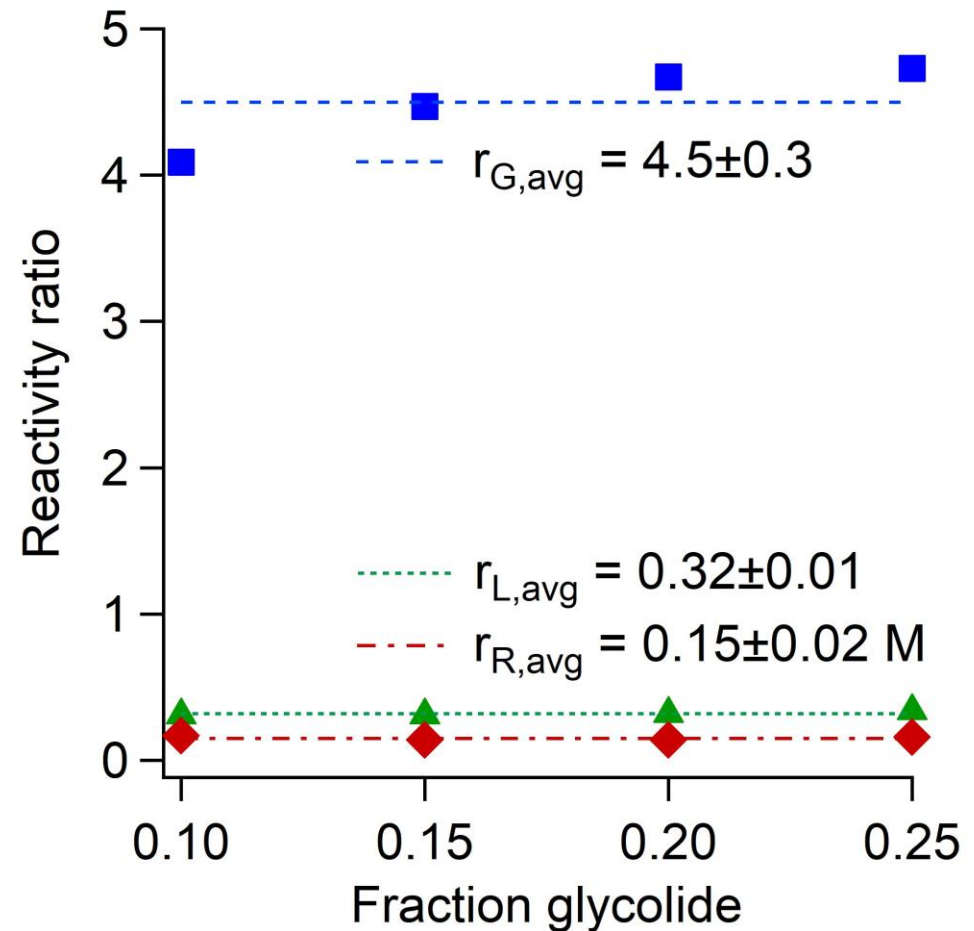
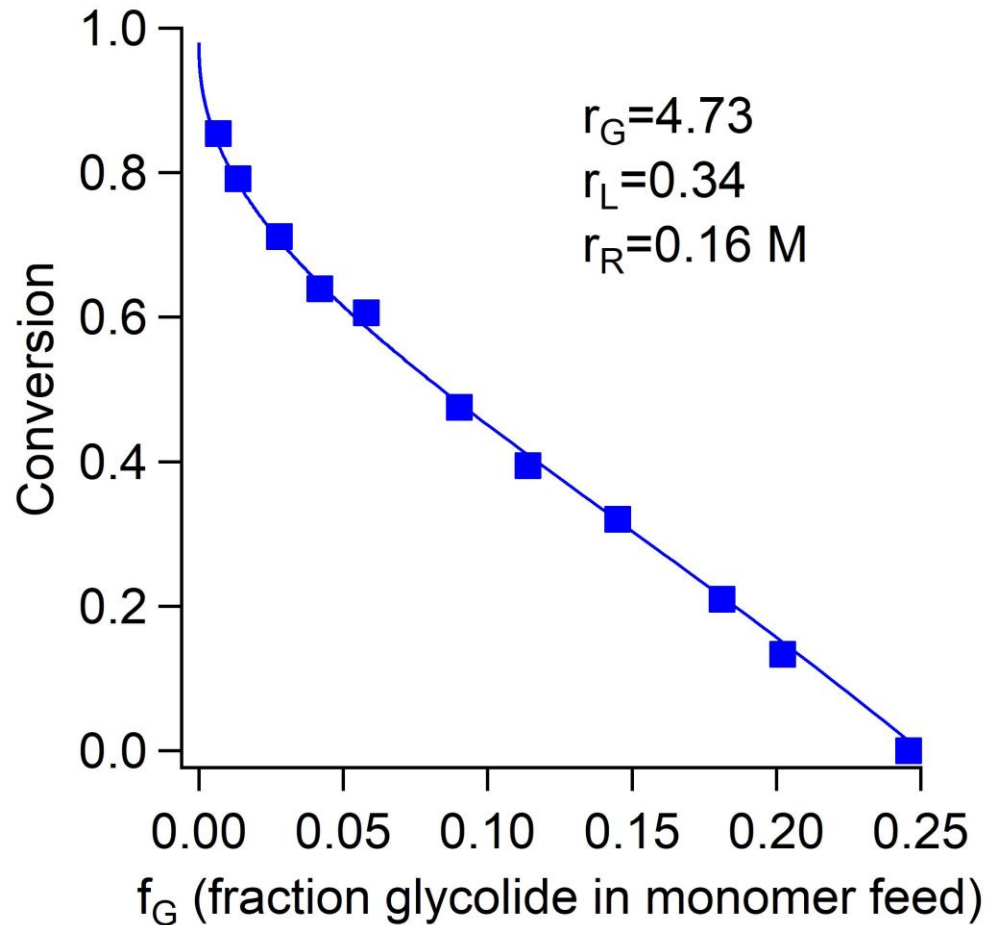
Increasing time/conversion

# $^1\text{H}$ NMR Spectroscopy was used to measure conversion

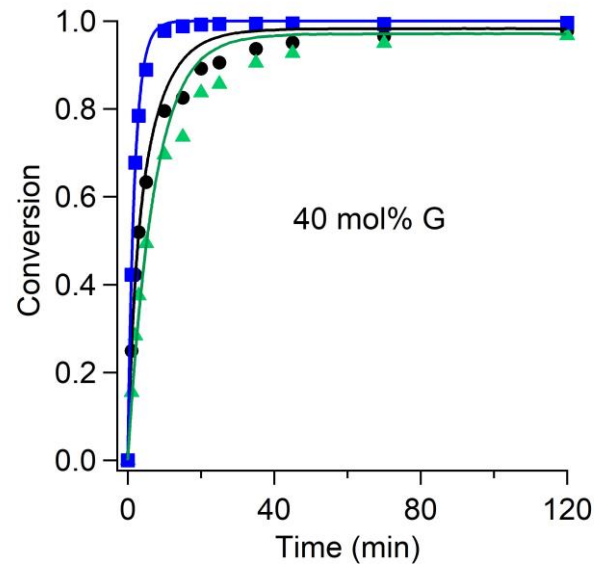
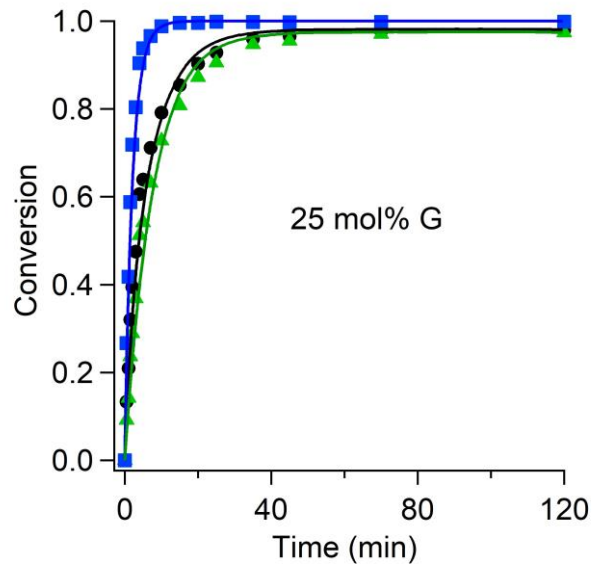
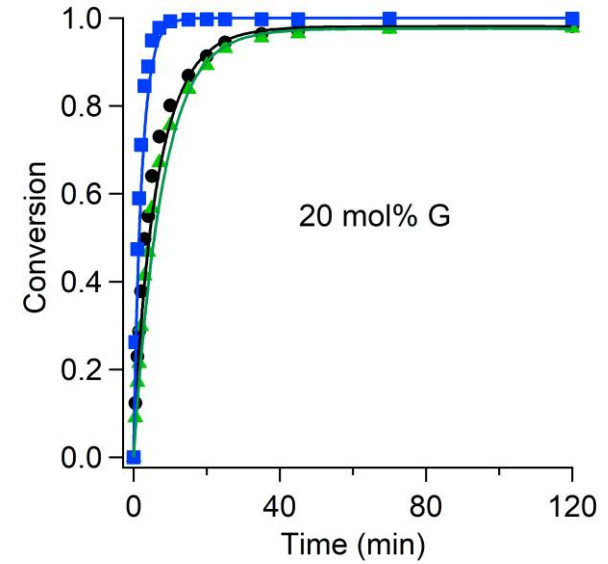
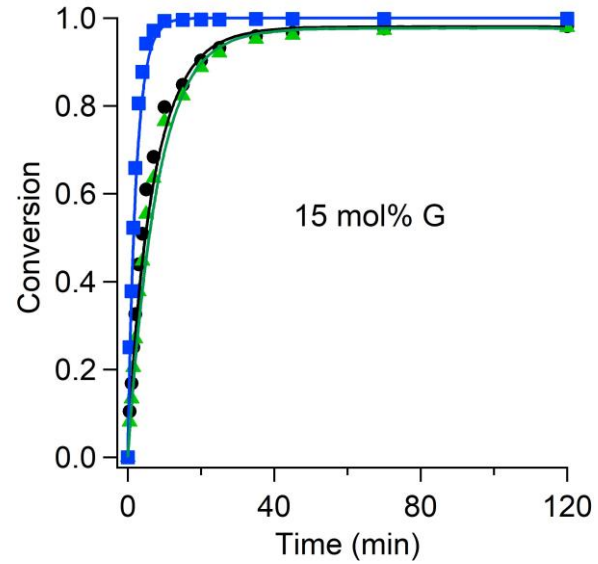
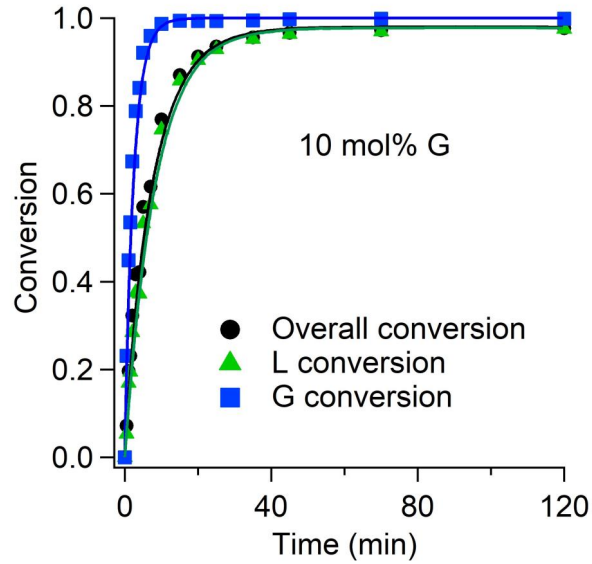




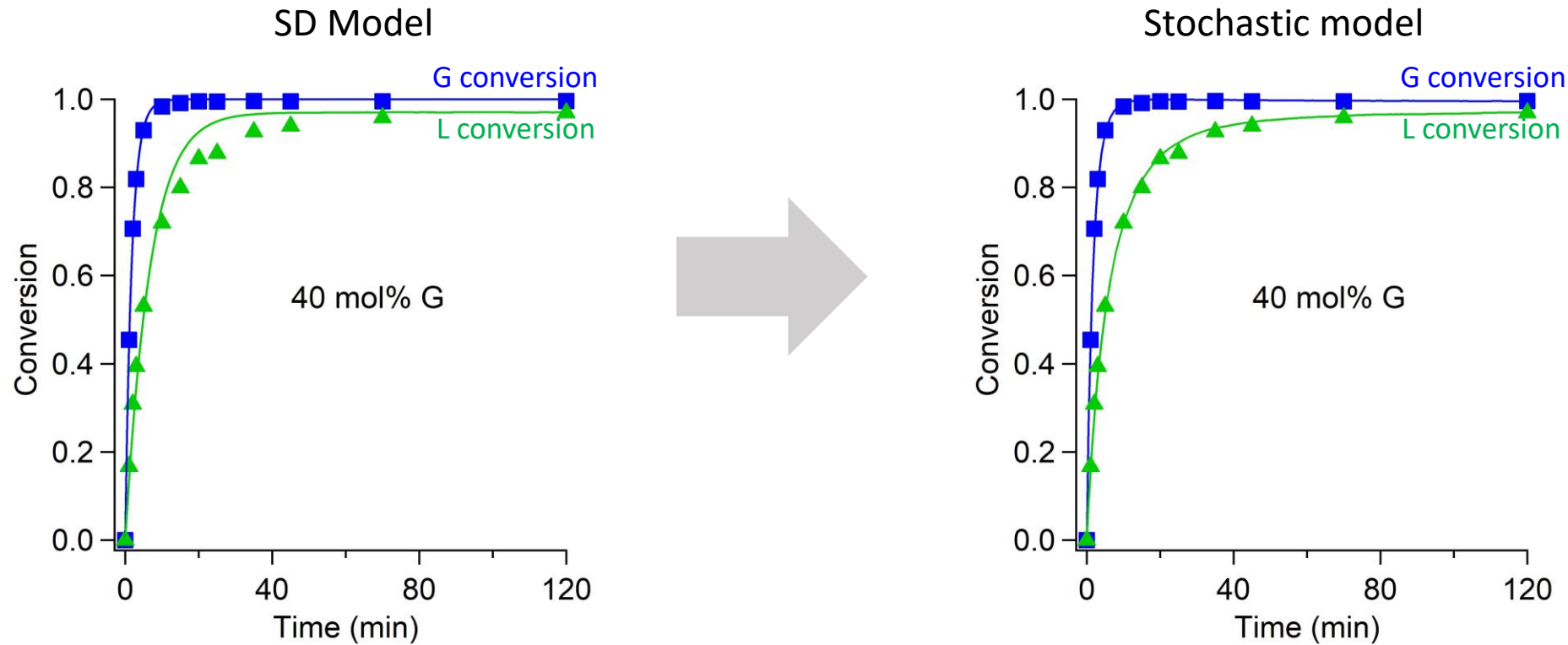
# Experimental data with low glycolide content was fit to the simplified deterministic model



# Stochastic modeling confirms accuracy of reactivity ratios



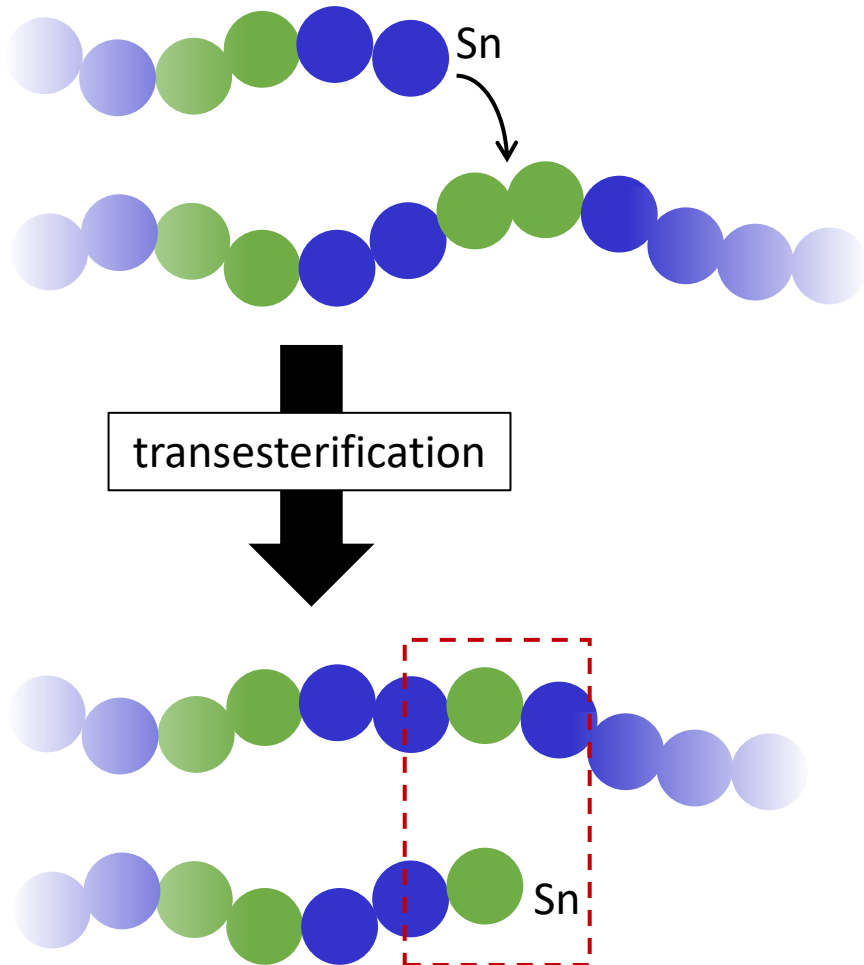
# Reactivity ratio accuracy can be improved by fitting directly to the stochastic model



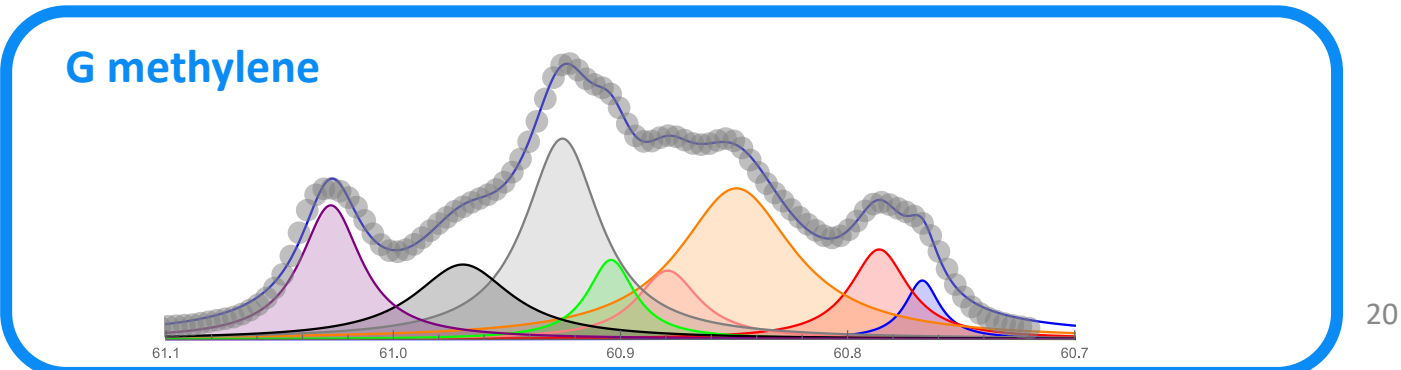
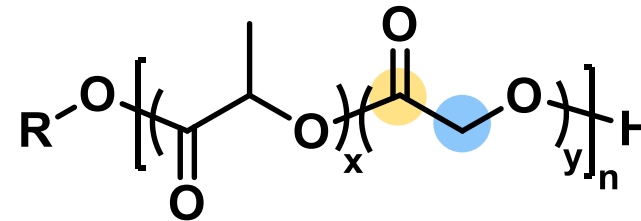
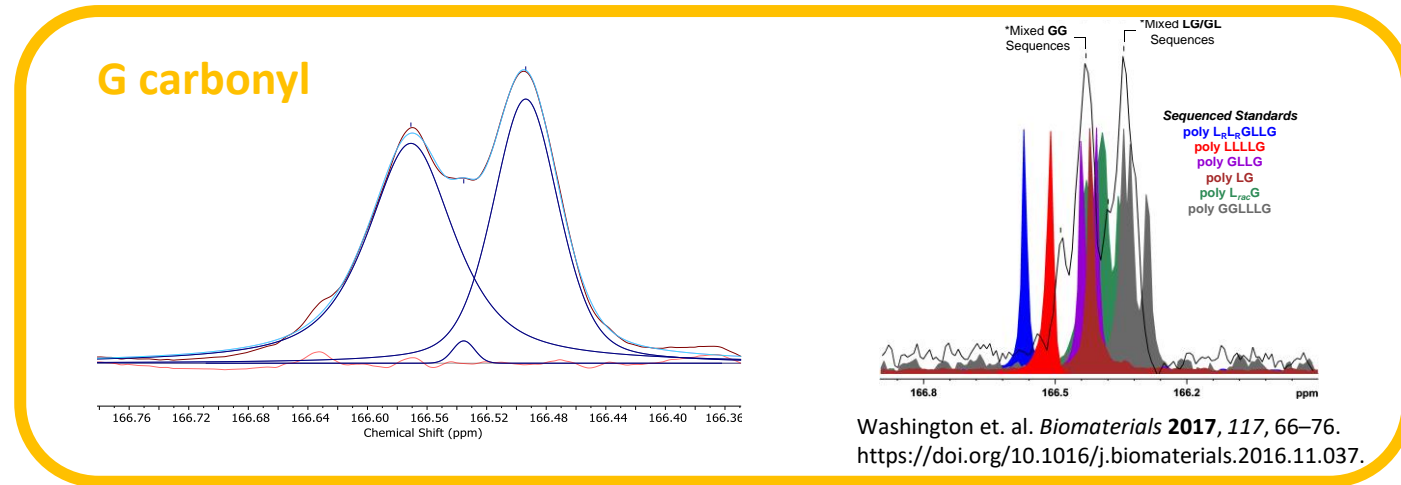
$$SSR(k_{GG}, k_{LG}, k_{LG}, k_{LL}, k_{G-G}, k_{G-L}, k_{L-G}, k_{L-L}) = \sum_{i=1}^{i=n_p} (p_G(t_i) - p_{G,i})^2 + \sum_{j=n_p+1}^{n_p+n'_p} (p_L(t_{j-n_p}) - p_{L,j-n_p})^2$$

# PLGA reactivity ratios alone don't solve all the problems

Transesterification has a major effect on PLGA sequencing but is not captured in reactivity ratios

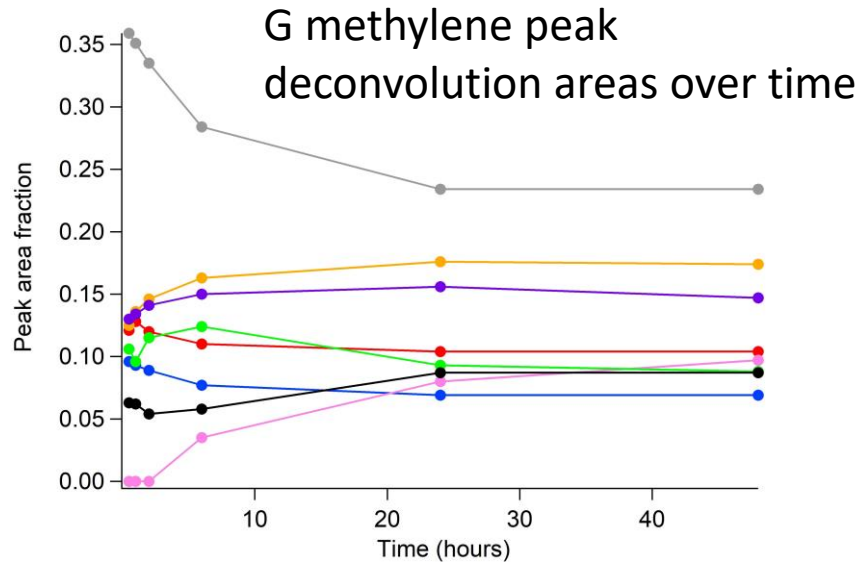


There is some disagreement about the best way to experimentally measure PLGA blockiness/sequence

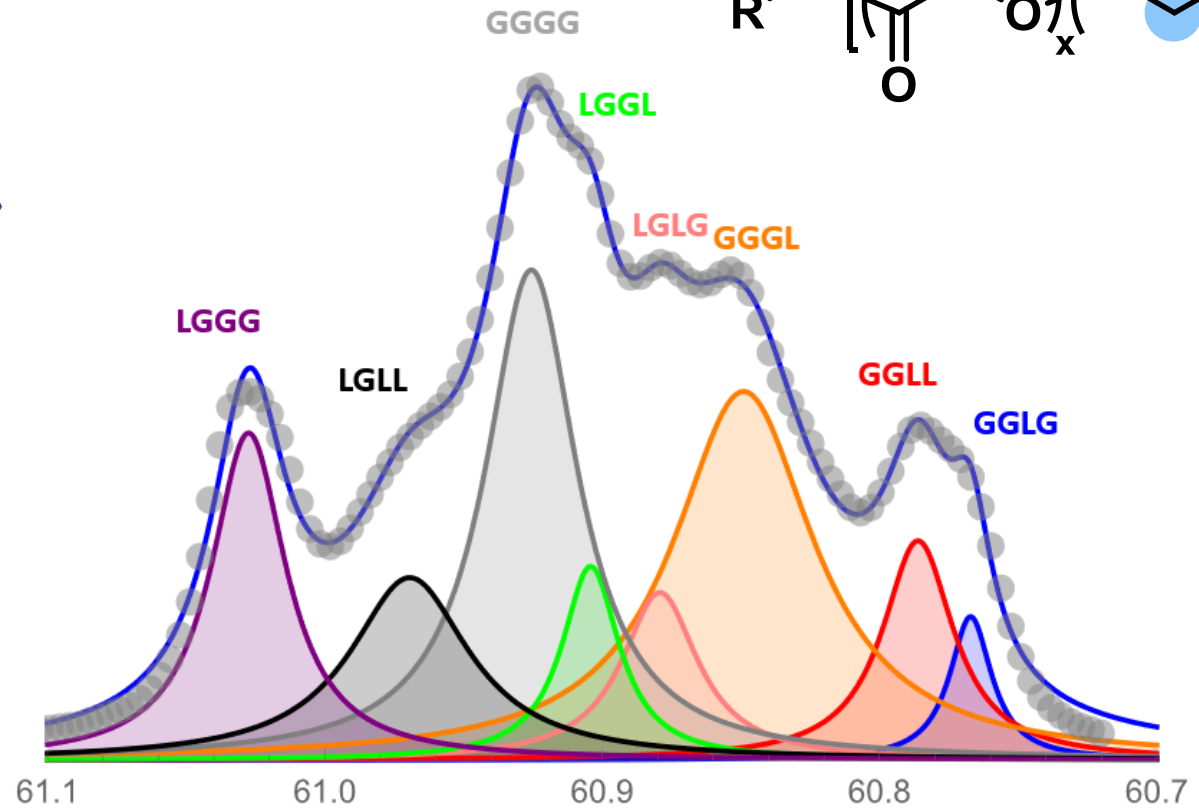
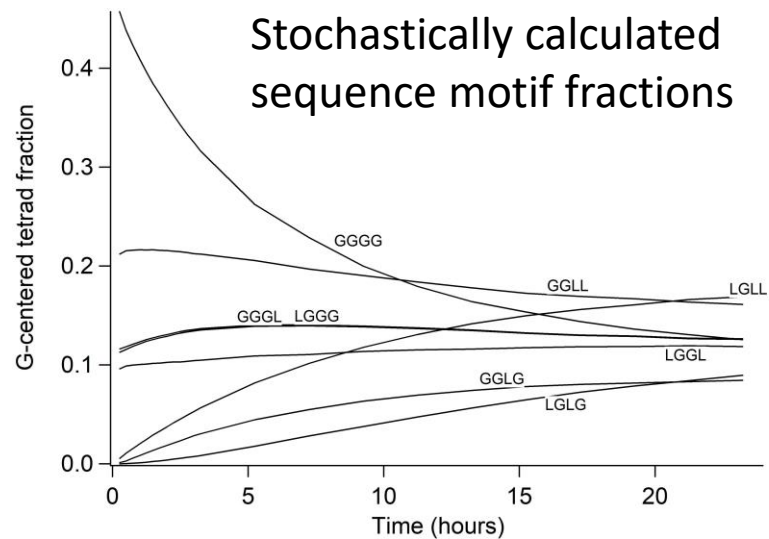
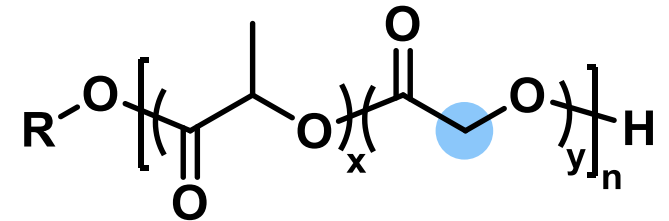




# We can further leverage the stochastic model to begin to solve these additional issues

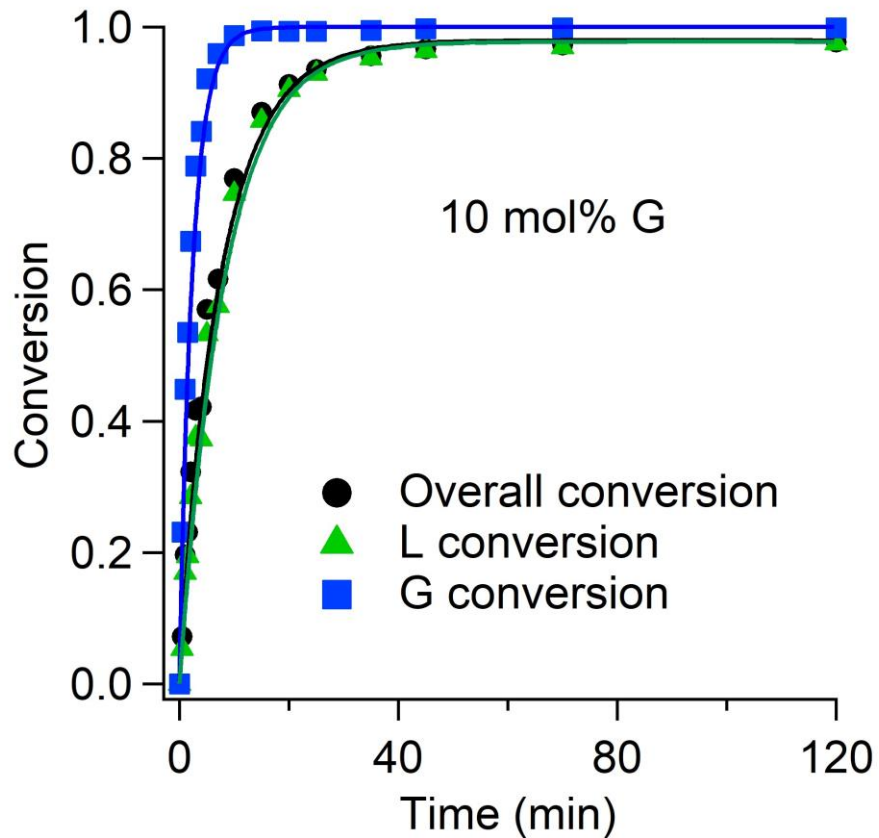


## Proposed glycolyl methylene peak assignments



# New fitting methods enable analysis of complex copolymerization kinetics and sequence

Reactivity ratio determination which accounts for reverse reactions



Complex  $^{13}\text{C}$  NMR peak assignment for improved experimental sequence measurement

